

RAIL-BRIDGE INTERACTION EFFECTS IN SINGLE-TRACK MULTI-SPAN BRIDGES. EXPERIMENTAL RESULTS VERSUS NUMERICAL PREDICTIONS UNDER OPERATING CONDITIONS

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Abstract. *This paper is devoted to the analysis of rail-bridge interaction effects in railway bridges under the circulation of moving trains. In a first approach, a bidimensional Finite Element model is implemented. The rail and the bridge are represented as Bernoulli-Euler beams, and a three-layer discrete track model accounting for the damping and flexibility of rail pads, ballast and subgrade is considered. In the model, several elastically supported spans are included, coupled by the presence of the track. First a sensitivity analysis is performed on the track parameters. A numerical receptance test is simulated on the rails showing that the track damping parameters influence the response only in the vicinity of the track natural frequencies, which are much higher than the bridge's. Then, the maximum acceleration of the bridge is evaluated under equidistant trains and consistent conclusions are extracted regarding the track parameters. Last, the number of spans included in the model is evaluated showing that limiting the model to one span does not necessarily lead to the highest response in terms of the bridge acceleration. Finally, the response of an existing two-span single-track bridge belonging to a conventional Spanish line is evaluated under the circulation of the Alaria Talgo train. Numerical predictions are compared to experimental results obtained in a recent campaign. The prediction of the vertical acceleration at the sensors located along the longitudinal symmetry axis is adequate. From the experimental results the coupling effect between the adjacent decks in each span is evident suggesting the need of analyzing this phenomenon with more sophisticated models.*

1 INTRODUCTION

Railway induced vibrations are a matter of concern for engineers and authorities in recent societies. In many countries, nowadays High-Speed services allow intense mobility between distant highly populated urban areas. The crescent density of traffic and the train operational speeds require, nonetheless, an outstanding response of railway infrastructures in order to ensure traffic safety, passenger comfort and adequate environmental conditions in the surrounding areas.

Comprising an important proportion of the railway infrastructure, railway bridges have received considerable attention in the last years and, to ensure traffic safety and passenger comfort, their design must accomplish strict requirements [1]. In particular, short-to-medium span simply-supported (SS) bridges with ballasted tracks are prone to experience high deck vertical accelerations which may lead to ballast deconsolidation, rail misalignment and other related problems [2]-[11]. In this context, a deep understanding of train-track-bridge interaction mechanisms is essential in order to be able to predict and assess the dynamic response of such structures. A state-of-the-art review on the evolution of numerical models and experimental tests focusing on validation, safety assessment and long-term performance investigation of train-track-bridge systems was recently presented by Zhai et al. [5].

Railway axle loads and bridges interact through the track infrastructure. The track distributes the axle loads and may exert a restraining effect on the bridges' boundary conditions [6] and a coupling effect among consecutive spans of the same viaduct [7], or between adjacent single-track decks [8]. Nevertheless, in many publications these effects are disregarded and the influence of the super-structure composed by the rails, sleepers and ballast, in ballasted tracks, is still not well known.

In this contribution, the dynamic behavior of multi-span single-track bridges is investigated with the aim of evaluating the effect of the continuity of the track on the bridge vertical response. In section 2 an existing bridge object of study is described, along with the numerical model. In section 3, the results of a preliminary sensitivity analysis on a few track parameters is presented. In section 4, the results of an experimental campaign recently performed on the bridge are compared with numerical predictions. Finally, some conclusions are extracted regarding the effect of the track super-structure on the bridge acceleration response.

2 BRIDGE DESCRIPTION AND NUMERICAL MODEL

2.1 Bridge description

The bridge under study is a bridge crossing the Old Guadiana River in the conventional railway line Madrid-Alcázar de San Juan-Jaén in the Alcázar de San Juan-Manzanares section (see Fig. 1). It is a double track concrete bridge composed by two identical SS bays. In each span, the horizontal structure is formed by two structurally independent decks, one for each track. Each deck is composed by a concrete slab resting on five pre-stressed concrete rectangular girders with no transverse stiffening elements (see Fig. 2). The longitudinal girders rest on the two abutments and on a central support through neoprene bearings. Each deck accommodates a ballasted track with Iberian gauge UIC60 rails and mono-block concrete sleepers with a spacing of 0.60 m.

2.2 Numerical model

In a first approach, the numerical model described in what follows is used. Only one single-track deck is represented in both bays as two successive Bernoulli-Euler (B-E) beams resting on elastic supports, accounting for the neoprene bearings elastic vertical stiffness. The two rails

2.3 Parameter selection and model updating

In the last years, different authors have proposed discrete track models for the analysis of railway induced vibrations. Fig. 4 shows the evident dispersity in the values of four parameters admitted in previous publications: the rail pads and ballast vertical stiffness and damping K_p , C_p , K_b and C_b . First, a set of nominal or reference values for all the track parameters is selected on the basis of the literature review. Then, the bridge parameters, assumed identical in both bays, (Modulus of Elasticity E_{bi} , moment of inertia I_{zbi} and linear mass m_{bi}) are adjusted in order to reproduce static and dynamic tests performed on the structure right before its opening [23]. In Table 1 the bridge and track reference parameters are included. These will be the ones used in the experimental validation (section 4). The fundamental frequency of the track-bridge system for these parameters equals 10.07 Hz. A damping ratio of 1.565% is assigned to any mode as per [24] for pre-stressed concrete bridges of the particular span length.

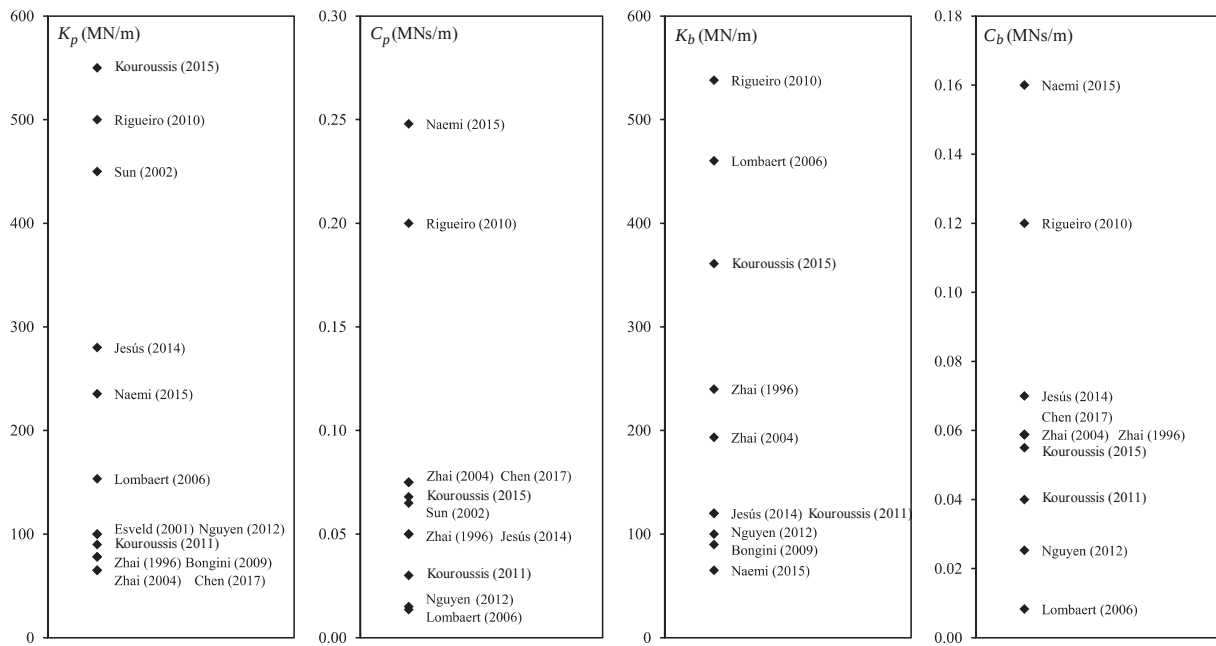


Figure 4: Rail pad and ballast layer stiffness and damping values admitted by different authors in the past for comparable ballast layers thicknesses and sleepers distances [6],[9]-[20].

Rail and bridge parameters		Track parameters per rail seat	
A_r (m ²)	76.86E-4	K_p (N/m)	1E8
E_r (Pa)	2.1E11	C_p (Ns/m)	7.5E4
I_{zr} (m ⁴)	3055E-8	M_{sl} (kg)	300
ρ_r (m ³)	7850	K_b (N/m)	1.933E8
D_{sl} (m)	0.60	C_b (Ns/m)	5.88E4
L_{bi} (m), N_{sp}	11.93, 2 spans	M_b (kg)	317.91
$(I_z \cdot E)_{bi}$ (Nm ²)	7.09E9	K_f (N/m)	7.3987E7
m_{bi} (kg/m)	8727	C_f (Ns/m)	3.115E4
ζ_{bi} (%)	1.565	K_w (N/m)	7.84E7
$K_{n,bi}$ (N/m) <i>st/dyn</i>	11.165E8 / 22.33E8	C_w (Ns/m)	8E4

Table 1: Bridge-track reference parameters

As per the subgrade stiffness and damping coefficients inside the bridge, $100 K_f$ and 0 Ns/m have been assigned as it is assumed that the ballast layer rests directly on the concrete slab.

A track length of 20 m is included before and after the two-span bridge, equivalent to more than 30 times the sleeper distance, which is considered adequate attending to previous publications [21], [22]. A convergence analysis is performed on this length ensuring the adequacy of this value.

3 SENSITIVITY ANALYSIS

3.1 Track receptance

First, the track dynamic response is evaluated numerically. To this end a harmonic test is performed on approximately 50 m of track (in the absence of bridge). A vertical harmonic load of 210 kN is applied at the central section of the double rail and the vertical displacement amplitude is determined in the same location. The forcing frequency varies between 1 and 2000 Hz in increments of 0.5 Hz. Fig. 5 shows the results for individual variations of C_p , C_b , C_f and C_w with respect to the reference values included in Table 1.

Two resonance frequencies are clearly detected in the proximities of 170 and 1350 Hz. The variations in the damping parameters affect the response only close to resonance. As the maximum frequency of interest in the bridge acceleration response is 60 Hz, the effect of these parameters on the bridge response should be very small. In the following section this particular issue is checked.

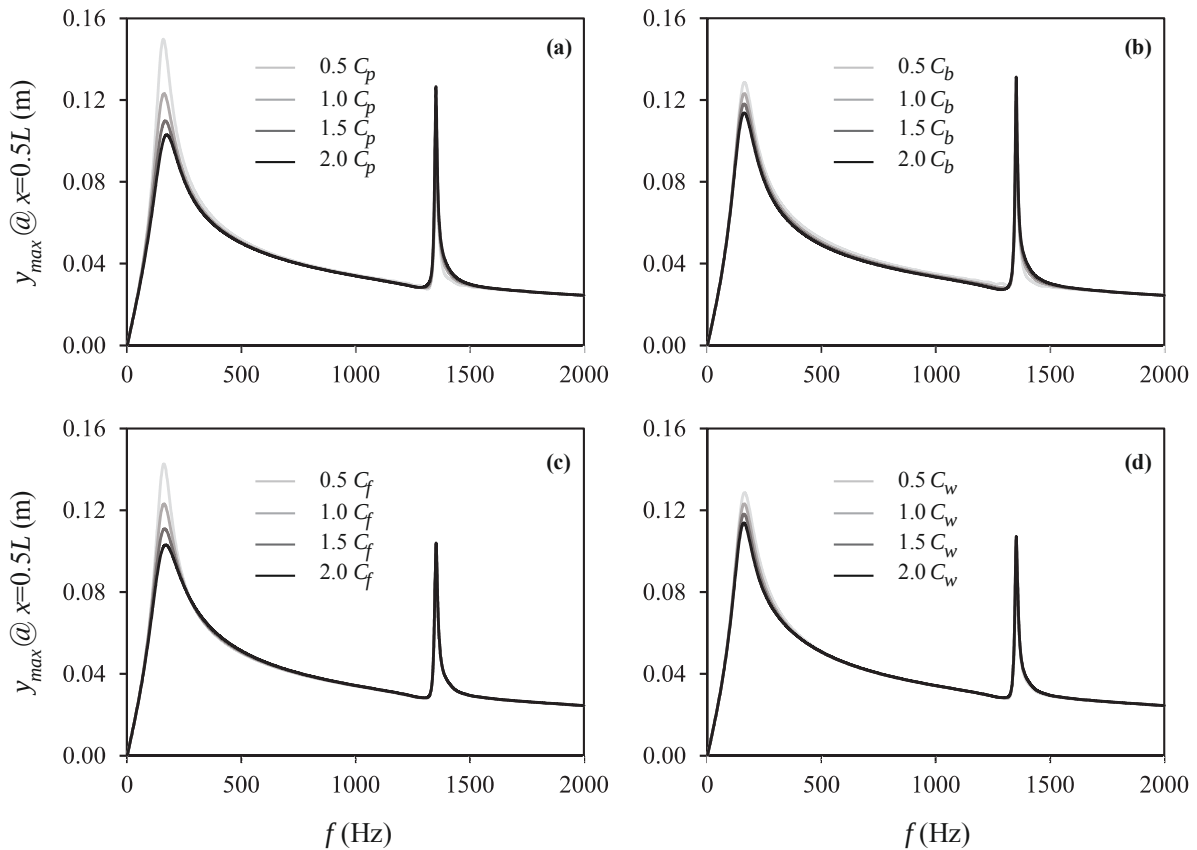


Figure 5: Receptance numerical test performed on the track model for independent variations of C_p , C_b , C_f and C_w .

3.2 Bridge maximum acceleration under train of equidistant loads

Second, the effect of the variations on four track parameters: the stiffness and damping coefficients of the rail pads, K_p and C_p , and of the ballast, K_b and C_b on the bridge maximum acceleration response is investigated. To this end, the response of the bridge is obtained under the circulation of an artificial train of 20 equidistant loads of 210 kN separated 18 m, with the aim of inducing two clear resonances on the structure. The bridge time-history response in terms of displacements and accelerations is obtained for 60 velocities of circulation in the range [40,100] m/s. A Chebyshev order 3 filter is applied to the acceleration response filtering contributions below 1 Hz and above 60 Hz. After filtering, maximum response envelopes are obtained for values of the track parameters:

$$[0.5, 1, 2, 4] \cdot K_p \quad [0, 0.5, 1, 2] \cdot C_p \quad [0.5, 1, 2, 4] \cdot K_b \quad [0, 0.5, 1, 2] \cdot C_b \quad (1)$$

where the values of K_p , C_p , K_b and C_b are those in Table 1. Fig. 6 shows the evolution of the maximum acceleration, which always takes place in the center of the second span, in absolute value in terms of the velocity for individual variations of each track parameter.

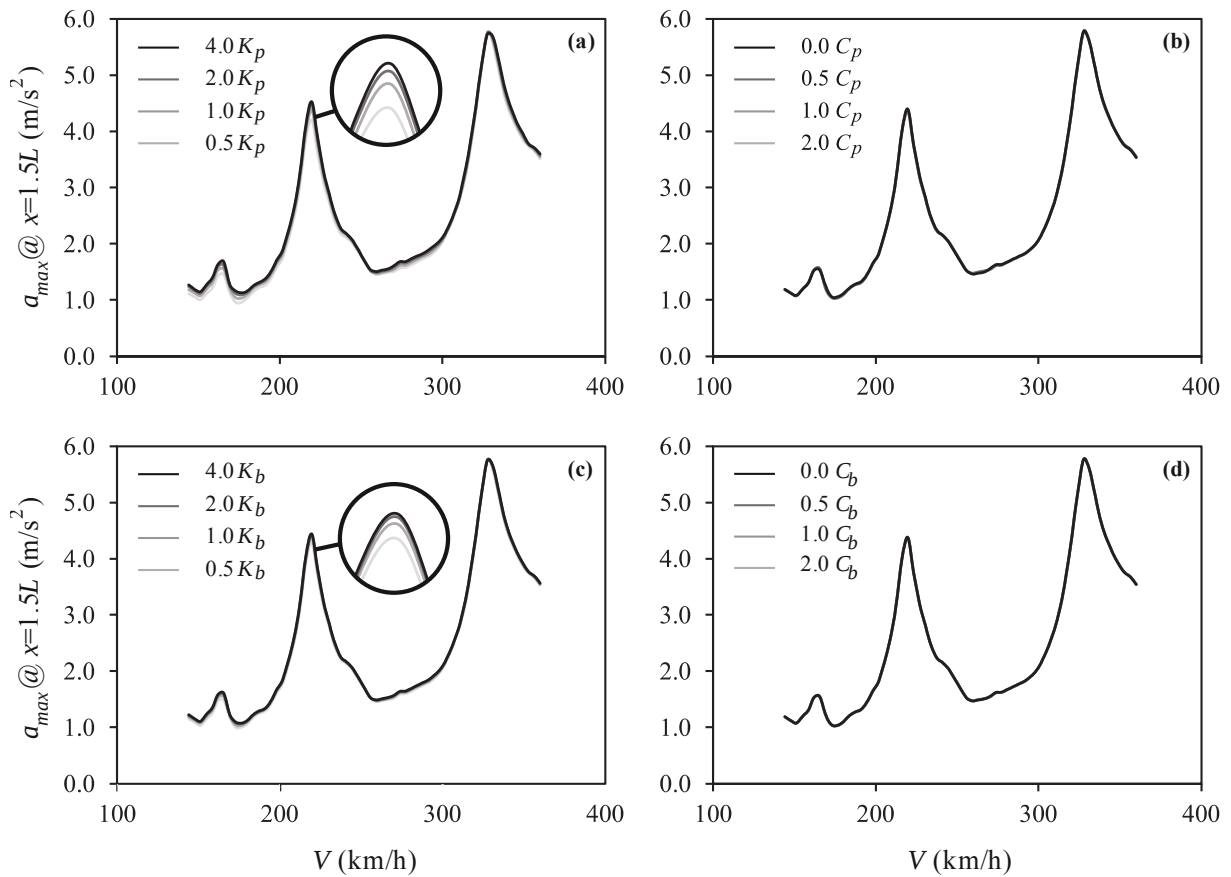


Figure 6: Maximum acceleration vs. velocity for individual variations of K_p , K_b , C_p , and C_b .

In all the plots shown in Fig. 6 three resonant peaks can be detected, corresponding to second, third and fourth resonances of the fundamental mode of the bridge, which in the reference case presents a frequency $f_1 = 10.07$ Hz. These theoretical resonant speeds can be calculated as:

$$V_1^{r,j=2} = \frac{df_1}{2} 3.6 = 326.27 \frac{\text{km}}{\text{h}} \quad V_1^{r,j=3} = 217.5 \frac{\text{km}}{\text{h}} \quad V_1^{r,j=4} = 163.1 \frac{\text{km}}{\text{h}} \quad (2)$$

The individual variations considered in the track do not affect significantly the reference fundamental frequency. From the observation of Fig. 6 (c)-(d) it may be concluded that the

influence of the variations in the rail pads and ballast damping constants is negligible on the maximum acceleration response of the bridge for the reference values of the remaining parameters, as expected from the results of the receptance study. The parameter that seems to affect the most the acceleration envelope at the most critical section is the rail pad stiffness K_p , leading to a decrease in the maximum acceleration at resonance as K_p reduces (for more flexible rail pads). This effect is more visible for higher resonance orders. The same tendencies, although in a less pronounced manner, are observed in terms of the variations considered in the ballast stiffness K_b .

3.3 Influence of the number of spans

Last in the sensitivity analysis, the effect of including a different number of spans in the numerical model on the maximum bridge response is investigated. Due to the longitudinal coupling exerted by the track on the structurally independent decks, the maximum response could differ depending on the number of spans. The analysis is performed in two cases: including and neglecting the decks neoprene bearings. In Fig. 7 the maximum acceleration at mid-span is represented for the same train of equidistant loads used in the previous subsection. All the bridge and track parameters adopt the reference values. Fig. 7(a) corresponds to the simply-supported (SS) case, i.e. no neoprene bearings, while Fig. 7(b) represents the elastically supported case, i.e. considering the neoprene bearings vertical flexibility. Colors red, black and grey are selected to represent results computed with one, two and three spans, respectively. Then, solid, dashed and dotted lines correspond to the response at mid-span of the first, second and third spans, respectively.

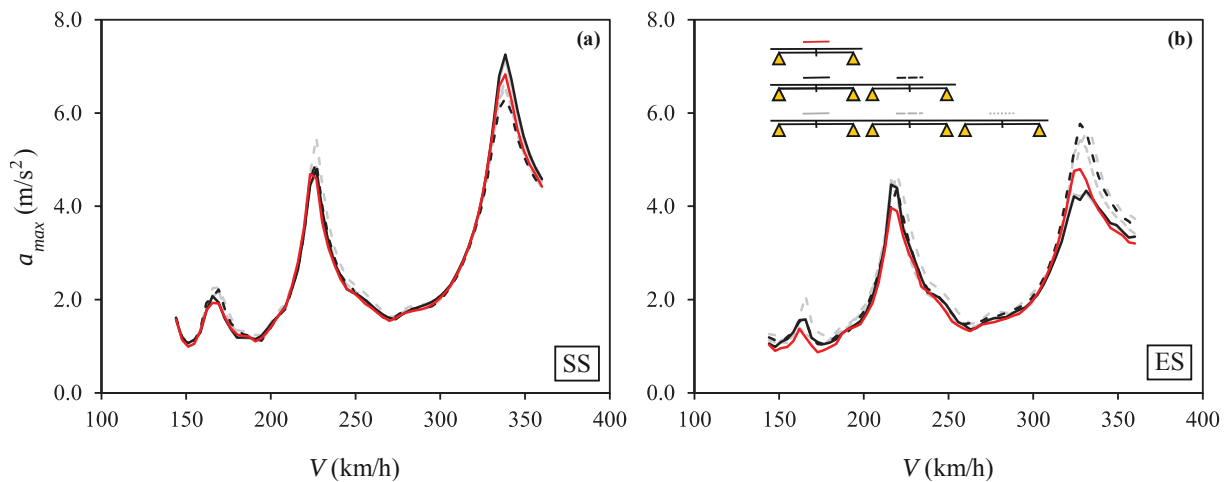


Figure 7: Maximum acceleration vs. velocity for models with one, two and three spans. (a) Simply-supported and (b) elastically-supported decks.

From the analysis of Fig. 7 one may conclude that: (i) the model leading to the maximum predicted acceleration and the most critical section depend on the maximum velocity considered; (ii) the difference between the three models is more relevant at resonance; (iii) in the particular case under study considering just one span does not predict the maximum response at any resonant peak. From the previously said, if the rail is included in the model and computational time is not an issue, including all the spans in the model may be on the safety side when it comes to predicting the maximum vertical acceleration response.

4.2 Numerical predictions vs. experimental measurements

During the campaign the response of the structure was recorded under the circulation of different trains. Two of these circulations are included in this section. Both correspond to the medium distance Renfe Altaria Talgo VI train travelling along tracks 2 and 1 (see Fig. 9) in the directions South-North (Manzanares-Alcázar de San Juan) and North-South, respectively. Fig. 10 and Fig. 11 show photographs of the trains and a scheme of the axles distances. Also, Table 2 includes the train axles arrangement and loads.

First, the speeds were identified from the frequency associated to the bogie distance leading to approximately 155 km/h in both cases. Then, the response of the bridge was calculated using the numerical model described in section 2.2 with the properties included in Table 1, with the exception of structural damping which was assumed as 3.1% for the fundamental frequency, 10.065 Hz, and 1.56% for 90 Hz (Eurocode value). The first value was identified during the proof load test. The numerical response, integrated in the time domain using the full FE model, is also filtered between 1 and 30 Hz, applying the same procedure as with the experimental records. Given the bidimensional nature of the numerical model, only the response at sensors installed underneath beams 3 and 8 is compared with the numerical predictions.



Figure 10: Renfe Altaria Talgo VI trains crossing Old Guadiana Bridge.

It has been verified that the bridge maximum acceleration did not exceed the limit established by the Serviceability Limit State for traffic safety in the case of ballasted tracks [1] according to the measurements in all the sensors.

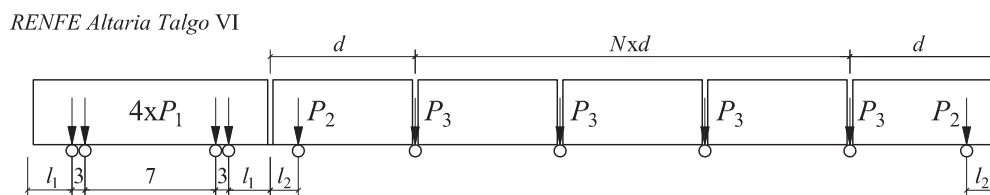


Figure 11: Renfe medium distance Altaria Talgo VI train axle scheme.

Train	N	d (m)	d_1 (m)	l_1 (m)	l_2 (m)	P_1 (kN)	P_2 (kN)	P_3 (kN)
Altaria	7	13.14	--	3.44	3.3	225	70	140

Table 2: RENFE Altaria Talgo VI features

Fig. 12 shows an experimental vs. numerical comparison of the vertical acceleration at sensors 5 and 6 under the circulation of the northbound train, in the time (a)-(b) and frequency (c)-(d) domains. The Talgo passenger coaches present a distance between shared axles of 13.14 m. The theoretical resonant speed associated to this length for the third resonance of the

fundamental mode is approximately 159 km/h, which is close to the real speed. This can be detected in the time-history plots where two oscillations of decreasing amplitude take place between the passage of consecutive axles.

$$V_1^{r,j=3} = \frac{df_1}{3} 3.6 = 158.7 \frac{\text{km}}{\text{h}} \approx 154.8 \frac{\text{km}}{\text{h}} = V \quad (3)$$

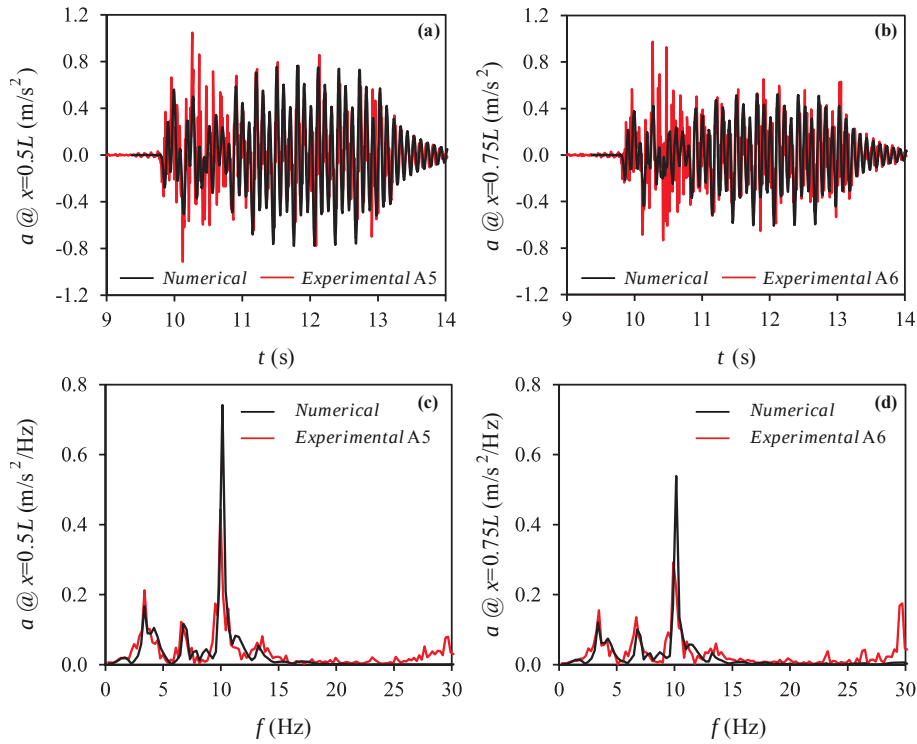


Figure 12: (a)-(b) Time history and (c)-(d) frequency content of the acceleration response at sensors 5 and 6 induced by Altaria Talgo VI train. Numerical prediction (black trace) vs. experimental measurements (red trace). Northbound train (track #2).

The accuracy of the numerical model is found reasonable up to 30 Hz, both at $L/2$ and $3L/4$ of the first span, although the numerical model overpredicts the acceleration for contributions close to the bridge fundamental frequency. This can be associated to vehicle-structure interaction which is not taken into account and can be of importance, specially at resonance; or to other energy dissipation mechanisms amplitude dependent such as the interaction between the adjacent decks, etc.

Fig. 13 shows the same type of comparative for the southbound train. In this case the acceleration is compared at sensors 13 and 17, located at mid-span of the second and first spans, respectively. Again, the time-history response is well reproduced, especially after the passage of the locomotive. In the frequency domain again, a predominant peak is detected showing the important contribution of the fundamental mode with a certain overprediction of the acceleration in the numerical case.

4.3 Coupling effect between adjoining decks

Finally, the coupling effect between the adjacent decks in each span is evaluated in forced vibration. Figs. 14(a)-(c) represent for the northbound train travelling along track #2 the experimental response measured at sensor 5 (at mid-span under the loaded track) and, simultaneously, at sensor 17 (at mid-span under the adjacent unloaded track).

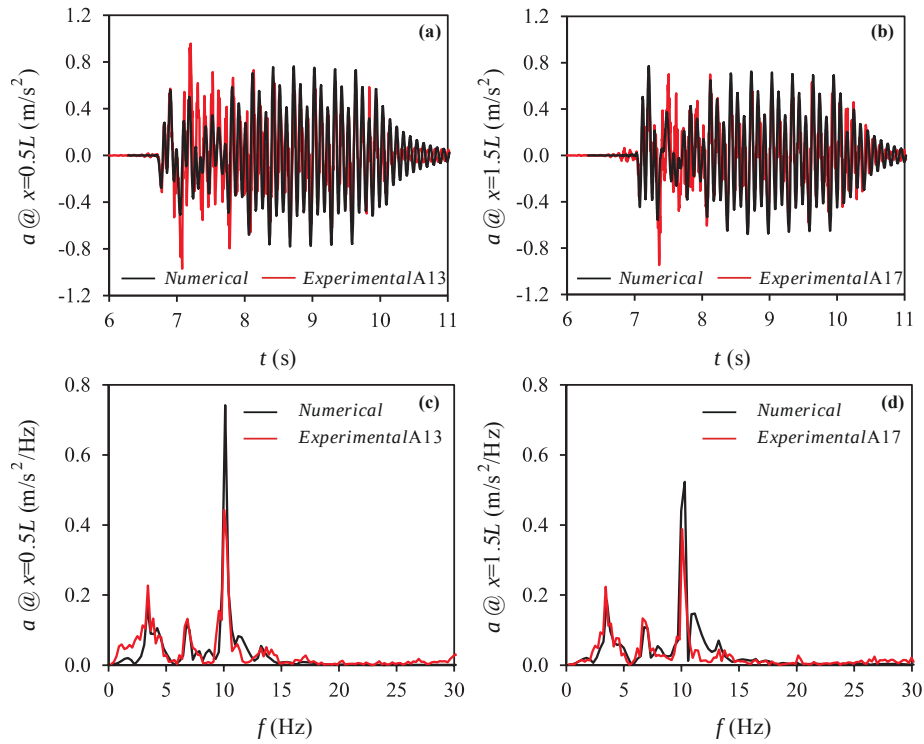


Figure 13: (a)-(b) Time history and (c)-(d) frequency content of the acceleration response at sensors 13 and 17 induced by Alaria Talgo VI train. Numerical prediction (black trace) vs. experimental measurements (red trace). Southbound train (track #1).

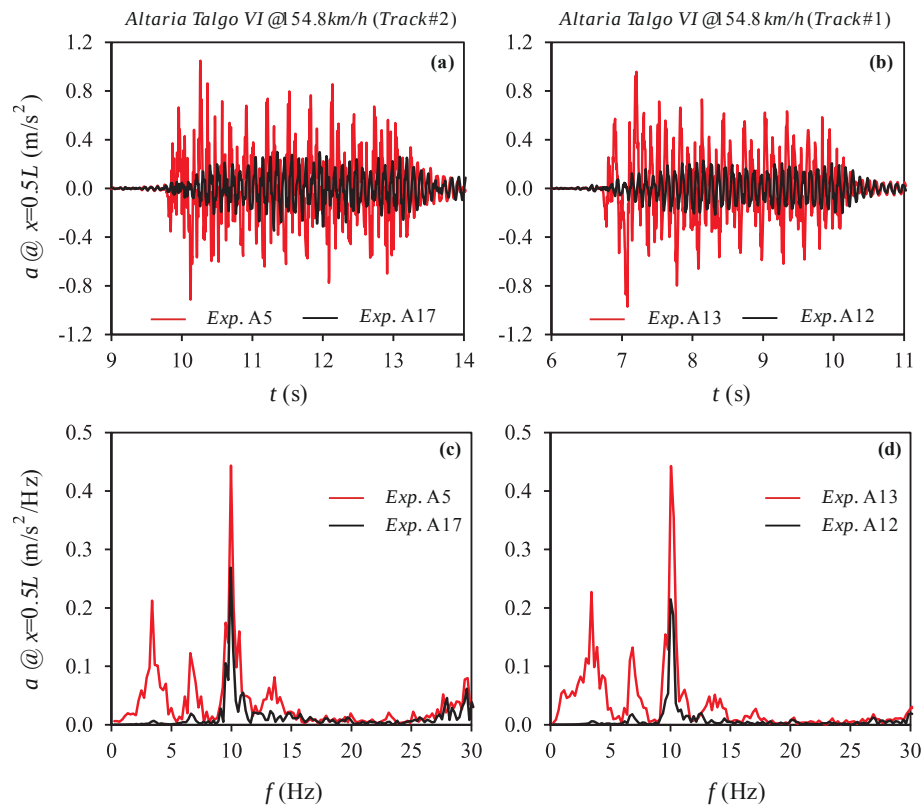


Figure 14: (a)-(b) Time history and (c)-(d) frequency content of the acceleration response at sensors 5 and 17 induced by the northbound train, and at sensors 13 and 12 induced by the southbound train.

The transmission of vibrations between the two decks is evident, even though these are only connected by the continuous ballast layer. At the unloaded sensor the frequency peaks associated to the excitation (e.g. bogie distance) which are visible in the low frequency range in the loaded sensor, are almost not perceptible; but the acceleration at the fundamental frequency reaches 60.6% of value in the loaded sensor. The same effect may be observed under the circulation of the southbound train when one compares the response between sensors 13 (under loaded track) and 12 (adjacent deck at symmetrical position). In this case the maximum acceleration in the unloaded sensor at the fundamental frequency in the frequency domain attains 48.5% the same maximum measured at sensor 13. This vibration transmission can be caused both by the continuous ballast layer and by the common foundations shared by the decks. In the opinion of the authors this phenomenon deserves further investigation. Implementing a 3D model of the bridge-track system would permit to evaluate the vibration transmitted between the decks close to the shared border in the frequency range of interest.

5 CONCLUSIONS

The present article constitutes a preliminary analysis on the longitudinal and transverse coupling effects exerted by the track on simply-supported bridges with independent single-track decks. From this study, the following can be concluded:

- There is a very high dispersion in the track parameters admitted by different authors for similar track infrastructures. The rail pad stiffness seems to affect the most the bridge maximum acceleration specially at high-order resonances, leading to lower amplitudes for higher flexibilities of this parameter. The ballast stiffness affects in a similar way, although to a lower extent. The damping parameters of the track do not seem to affect the bridge maximum response below 60 Hz. These parameters do affect the track response but at much higher frequencies.
- Considering one span in multi-span bridges may not lead to the maximum predicted acceleration when the track is included in the numerical model. The effect of the number of spans gains importance at resonance. The model leading to the maximum dynamic response as well as the most critical section depend on the maximum velocity of interest.
- The experimental vs. numerical predictions in the case of Old Guadiana bridge are reasonable in the sensors located along the longitudinal axis of the decks, as there is no contribution of the torsion mode at those locations. The numerical model tends to overestimate the real response close to the bridge natural frequency.
- The transmission of vibrations from the loaded deck to the unloaded deck is relevant. This may be caused by the continuous ballast layer but also by the shared foundations of the two decks. In the authors' opinion this effect is not well known and should be investigated using a 3D model of the complete bridge.

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