

Supporting Information for

Evaluating Enhanced Sulfate Reduction and Optimized Volatile Fatty Acids (VFA)

Composition in Anaerobic Reactor by Fe (III) Addition

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Table S1. The Definition and Units of Model Components

Variable	Definition	Unit
S_{su}	Sugar	g COD/m ³
S_{bu}	Butyrate acid	g COD/m ³
S_{bu-}	Butyrate	g COD/m ³
S_{pro}	Propionate acid	g COD/m ³
S_{pro-}	Propionate	g COD/m ³
S_{ac}	Acetate acid	g COD/m ³
S_{ac-}	Acetate	g COD/m ³
S_{h2}	Hydrogen in wastewater	g COD/m ³
$S_{h2,g}$	Hydrogen in gas phase	g COD/m ³
S_{co2}	Carbon dioxide in wastewater	mM
S_{hco3}	Bicarbonate	mM
$S_{co2,g}$	Carbon dioxide in gas phase	mM
S_{nh3}	Ammonia	g N/m ³
S_{nh4}	Ammonium	g N/m ³
S_{SO4}	Sulfate	g S/m ³
S_{H2S}	H ₂ S in wastewater	g S/m ³
S_{HS}	HS ⁻ in wastewater	g S/m ³
$S_{H2S,g}$	H ₂ S in gas phase	g S/m ³
S_{h+}	Hydrogen ion	mM
S_{Cat}	Metallic cation	mM
S_{An}	Metallic anion	mM
S_{Fe2}	Fe ²⁺	g Fe/m ³
X_{Fe3}	Fe ₂ O ₃	g Fe/m ³
S_{Fe3}	Fe ³⁺	g Fe/m ³
X_{FeS}	Iron-sulfide precipitation	g /m ³
X_S	Readily biodegradable COD	g COD/m ³
X_I	Inert particular COD	g COD/m ³
X_{su}	Sugar degraders	g COD/m ³
X_{bu}	Butyrate degraders	g COD/m ³
X_{pro}	Propionate degraders	g COD/m ³
$X_{IRB,bu}$	IRB grown on butyrate	g COD/m ³
$X_{IRB,pro}$	IRB grown on propionate	g COD/m ³
$X_{IRB,ac}$	IRB grown on acetate	g COD/m ³
$X_{IRB,h}$	IRB grown on hydrogen	g COD/m ³
$X_{SRB,bu}$	SRB grown on butyrate	g COD/m ³
$X_{SRB,pr}$	SRB grown on propionate	g COD/m ³
$X_{SRB,ac}$	SRB grown on acetate	g COD/m ³
$X_{SRB,h}$	SRB grown on hydrogen	g COD/m ³
S_{IC}	Total inorganic carbon	mM
S_{IN}	Total inorganic nitrogen	g N/m ³
S_{oH-}	Hydroxide ion	mM

Table S2. Stoichiometric Matrix for the Developed Model

	S_{su}	S_{bu}	S_{pro}	S_{ac}	S_{h2}	S_{SO4}	S_{H2S}	S_{IC}	S_{IN}	X_{Fe3}	S_{Fe3}	S_{Fe2}	X_{FeS}	X_S	X_I	X_{su}	X_{bu}	X_{pro}	$X_{SRB,bu}$	$X_{SRB,pr}$	$X_{SRB,ac}$	$X_{SRB,h}$	$X_{IRB,bu}$	$X_{IRB,pr}$	$X_{IRB,ac}$	$X_{IRB,h}$	
	COD	COD	COD	COD	COD	S	S	C	N	Fe	Fe	Fe	FeS	COD	COD	COD	COD	COD	COD	COD	COD	COD	COD	COD	COD	COD	COD
1	1													-1													
2	-1	$f1(1-Y_{su})$	$f2(1-Y_{su})$	$f3(1-Y_{su})$	$f4(1-Y_{su})$			$-\sum c(C_i) \cdot v_{i,a}$	$-Y_{su}c(N_{bio})$							Y_{su}											
3		-1	$f5(1-Y_{bu})$	$f6(1-Y_{bu})$					$-Y_{c4}c(N_{bio})$								Y_{bu}										
4			-1	$f7(1-Y_{pro})$	$f8(1-Y_{pro})$			$-\sum c(C_i) \cdot v_{i,a}$	$-Y_{pr}c(N_{bio})$									Y_{pro}									
5		-1				$-\frac{1-Y_{SRB,bu}}{2}$	$\frac{1-Y_{SRB,bu}}{2}$		$-Y_{SRB,bu}c(N_{bio})$										$Y_{SRB,bu}$								
6			-1			$-\frac{1-Y_{SRB,pr}}{2}$	$\frac{1-Y_{SRB,pr}}{2}$	$-\sum c(C_i) \cdot v_{i,a}$	$-Y_{SRB,pr}c(N_{bio})$											$Y_{SRB,pr}$							
7				-1		$-\frac{1-Y_{SRB,ac}}{2}$	$\frac{1-Y_{SRB,ac}}{2}$	$-\sum c(C_i) \cdot v_{i,a}$	$-Y_{SRB,ac}c(N_{bio})$												$Y_{SRB,ac}$						
8					-1	$-\frac{1-Y_{SRB,h}}{2}$	$\frac{1-Y_{SRB,h}}{2}$	$-\sum c(C_i) \cdot v_{i,a}$	$-Y_{SRB,h}c(N_{bio})$													$Y_{SRB,h}$					
9		-1							$-Y_{IRB}c(N_{bio})$	$-7(1-Y_{IRB})$	$7(1-Y_{IRB})$												Y_{IRB}				
10			-1					$-\sum c(C_i) \cdot v_{i,a}$	$-Y_{IRB}c(N_{bio})$	$-7(1-Y_{IRB})$	$7(1-Y_{IRB})$												Y_{IRB}				
11				-1				$-\sum c(C_i) \cdot v_{i,a}$	$-Y_{IRB}c(N_{bio})$	$-7(1-Y_{IRB})$	$7(1-Y_{IRB})$													Y_{IRB}			
12					-1			$-\sum c(C_i) \cdot v_{i,a}$	$-Y_{IRB}c(N_{bio})$	$-7(1-Y_{IRB})$	$7(1-Y_{IRB})$															Y_{IRB}	
13										-1	1																
14							-1					$-\eta1$	$\eta2$														
15														0.9	0.1	-1											
16														0.9	0.1		-1										
17														0.9	0.1			-1									
18														0.9	0.1				-1								
19														0.9	0.1					-1							
20														0.9	0.1						-1						
21														0.9	0.1							-1					
22														0.9	0.1								-1				
23														0.9	0.1									-1			
24														0.9	0.1										-1		
25														0.9	0.1												-1

Table S3. Process Kinetic Rate Equations for the Developed Model

Process	Kinetics rates expressions
1. Hydrolysis	$k_{hydro} X_{su}$
2. Uptake of sugar	$k_{su} \frac{S_{su}}{K_{su} + S_{su}} X_{su} I_1$
3. Uptake of butyrate acid	$k_{bu} \frac{S_{bu}}{K_{bu} + S_{bu}} X_{bu} I_2 I_{h2s,bu}$
4. Uptake of propionate acid	$k_{pro} \frac{S_{pro}}{K_{pro} + S_{pro}} X_{pro} I_2 I_{h2s,pro}$
5. Butyrate-based sulfidogenesis	$k_{SRB,bu} \frac{S_{bu}}{K_{SRB,bu} + S_{bu}} \frac{S_{SO4}}{K_{SO4} + S_{SO4}} X_{SRB,bu} I_{pH} I_{h2s,SRB,bu} P_{Fe3}$
6. Propionate-based sulfidogenesis	$k_{SRB,pro} \frac{S_{pro}}{K_{SRB,pro} + S_{pro}} \frac{S_{SO4}}{K_{SO4} + S_{SO4}} X_{SRB,pro} I_{pH} I_{h2s,SRB,pro} P_{Fe3}$
7. Acetate-based sulfidogenesis	$k_{SRB,ac} \frac{S_{ac}}{K_{SRB,ac} + S_{ac}} \frac{S_{SO4}}{K_{SO4} + S_{SO4}} X_{SRB,ac} I_{pH} I_{h2s,SRB,ac} P_{Fe3}$
8. Hydrogenotrophic sulfidogenesis	$k_{SRB,h} \frac{S_h}{K_{SRB,h} + S_h} \frac{S_{SO4}}{K_{SO4} + S_{SO4}} X_{SRB,h} I_{pH} I_{h2s,SRB,h} P_{Fe3}$
9. Butyrate-based iron reduction	$k_{IRB,bu} \frac{S_{bu}}{K_{IRB,bu} + S_{bu}} \frac{S_{Fe3}}{K_{Fe3^+} + S_{Fe3}} X_{IRB,bu} I_{pH} I_{h2s,IRB}$
10. Propionate-based iron reduction	$k_{IRB,pro} \frac{S_{pro}}{K_{IRB,pro} + S_{pro}} \frac{S_{Fe3}}{K_{Fe3^+} + S_{Fe3}} X_{IRB,pro} I_{pH} I_{h2s,IRB}$
11. Acetate-based iron reduction	$k_{IRB,ac} \frac{S_{ac}}{K_{IRB,ac} + S_{ac}} \frac{S_{Fe3}}{K_{Fe3^+} + S_{Fe3}} X_{IRB,ac} I_{pH} I_{h2s,IRB}$
12. Hydrogenotrophic iron reduction	$k_{IRB,h} \frac{S_h}{K_{IRB,h} + S_h} \frac{S_{Fe3}}{K_{Fe3^+} + S_{Fe3}} X_{IRB,h} I_{pH} I_{h2s,IRB}$
13. Fe ₂ O ₃ corrosion	$k_{Fe} \frac{X_{Fe3}}{K_{Fe3} + X_{Fe3}}$
14. Sulfide precipitation	$k_{pre} S_{H2S} S_{Fe2}$

15. Decay of X_{su}	$k_{dec,su} X_{su}$
16. Decay of X_{bu}	$k_{dec,bu} X_{bu}$
17. Decay of X_{pro}	$k_{dec,pro} X_{pro}$
18. Decay of $X_{SRB,bu}$	$k_{dec,SRB,bu} X_{SRB,bu}$
19. Decay of $X_{SRB,pr}$	$k_{dec,SRB,pro} X_{SRB,pro}$
20. Decay of $X_{SRB,ac}$	$k_{dec,SRB,ac} X_{SRB,ac}$
21. Decay of $X_{SRB,h}$	$k_{dec,SRB,h} X_{SRB,h}$
22. Decay of $X_{IRB,bu}$	$k_{dec,IRB} X_{IRB,bu}$
23. Decay of $X_{IRB,pr}$	$k_{dec,IRB} X_{IRB,pro}$
24. Decay of $X_{IRB,ac}$	$k_{dec,IRB} X_{IRB,ac}$
25. Decay of $X_{IRB,h}$	$k_{dec,IRB} X_{IRB,h}$
$P_{fe3} = \frac{X_{fe3}}{K_{p,fe}} + 1 \quad \text{and} \quad I_{h2s} = 1 - \frac{S_{h2s}}{K_{h2s}}$	

Table S4. Acid-base Reactions of the Developed Model

Equation
$S_{Cat} + S_{nh4}/14 + S_{h+} 2 * S_{Fe2} + 3 * S_{Fe3} - S_{hco3} - S_{ac-}/64 - S_{pro-}/112 - S_{bu-}/160 - S_{oH-} - 2 * S_{SO4}/32 - S_{HS}/32 - S_{An} = 0$
$S_{oH-} * S_{h+} = Kw$
$S_{bu-} * (K_{a,bu+} S_{h+}) - K_{a,bu+} (S_{bu-} + S_{bu}) = 0$
$S_{pro-} * (K_{a,pro+} S_{h+}) - K_{a,pro+} (S_{pro-} + S_{pro}) = 0$
$S_{ac-} * (K_{a,ac+} S_{h+}) - K_{a,ac+} (S_{ac-} + S_{ac}) = 0$
$S_{hco3-} * (K_{a,co2+} S_{h+}) - K_{a,co2+} (S_{hco3-} + S_{co2}) = 0$
$S_{nh4-} * (K_{a,nh4+} S_{h+}) - K_{a,nh4+} (S_{nh4} + S_{nh3}) = 0$
$S_{hs-} * (K_{a,h2s+} S_{h+}) - K_{a,h2s+} (S_{hs-} + S_{h2s}) = 0$

Table S5. Liquid Phase Yield Coefficient and Rate Equations for Liquid-Gas Reactions in the Developed Model

	S_{h2} COD	S_{co2} C	S_{h2s} S	<i>Rate</i>
1	-1			$k_L a(S_{h2} - K_{H,h2} RTS_{h2,g})$
2		-1		$k_L a(S_{co2} - K_{H,co2} RTS_{co2,g})$
3			-1	$k_L a(S_{h2s} - K_{H,h2s} RTS_{h2s,g})$

Table S6. Kinetic and Stoichiometric Parameters of the Developed Model

Parameter	Definition	Values	Unit	Source
k_{hydro}	Hydrolysis rate of X_s	1	d^{-1}	(1)
k_{su}	Maximum uptake rate of S_{su} by X_{su}	10	$\frac{g\ COD\ m^{-3}\ _S}{g\ COD\ m^{-3}\ _X\ d^{-1}}$	(2)
K_{su}	Half saturation constant for S_{su}	1000	$g\ COD\ m^{-3}$	(2)
k_{bu}	Maximum uptake rate of S_{bu} by X_{bu}	5	$\frac{g\ COD\ m^{-3}\ _S}{g\ COD\ m^{-3}\ _X\ d^{-1}}$	(2)
K_{bu}	Half saturation constant for S_{bu}	500	$g\ COD\ m^{-3}$	(2)
k_{pro}	Maximum uptake rate of S_{pro} by X_{pro}	5	$\frac{g\ COD\ m^{-3}\ _S}{g\ COD\ m^{-3}\ _X\ d^{-1}}$	(2)
K_{pro}	Half saturation constant for S_{pro}	500	$g\ COD\ m^{-3}$	(2)
$k_{SRB,bu}$	Maximum uptake rate of S_{bu} by $X_{SRB,bu}$	13.7	$\frac{g\ COD\ m^{-3}\ _S}{g\ COD\ m^{-3}\ _X\ d^{-1}}$	(3)
$K_{SRB,bu}$	Half saturation constant of $X_{SRB,bu}$ for S_{bu}	100	$g\ COD\ m^{-3}$	(3)
$k_{SRB,pro}$	Maximum uptake rate of S_{pro} by $X_{SRB,pro}$	13.6	$\frac{g\ COD\ m^{-3}\ _S}{g\ COD\ m^{-3}\ _X\ d^{-1}}$	(3)
$K_{SRB,pro}$	Half saturation constant of $X_{SRB,pro}$ for S_{pro}	150	$g\ COD\ m^{-3}$	(3)
$k_{SRB,ac}$	Maximum uptake rate of S_{ac} by $X_{SRB,ac}$	13.9	$\frac{g\ COD\ m^{-3}\ _S}{g\ COD\ m^{-3}\ _X\ d^{-1}}$	(3)
$K_{SRB,ac}$	Half saturation constant of $X_{SRB,ac}$ for S_{ac}	150	$g\ COD\ m^{-3}$	(3)
$k_{SRB,h}$	Maximum uptake rate of S_h by $X_{SRB,h}$	26.7	$\frac{g\ COD\ m^{-3}\ _S}{g\ COD\ m^{-3}\ _X\ d^{-1}}$	(3)
$K_{SRB,h}$	Half saturation constant of $X_{SRB,h}$ for S_h	0.1	$g\ COD\ m^{-3}$	(3)
K_{SO4}	Half saturation constant for S_{SO4}	64	$g\ S\ m^{-3}$	(3)
k_{Fe}	Maximum uptake rate of Fe_2O_3	40	$g\ Fe\ m^{-3}$	(4)
K_{Fe3}	Uptake affinity constant for Fe_2O_3	1000	$g\ Fe\ m^{-3}$	(4)
$K_{P,Fe}$	Promotion constant of Fe_2O_3	7000	$g\ Fe\ m^{-3}$	(4)
$k_{IRB,bu}$	Maximum uptake rate of S_{bu} by $X_{IRB,bu}$	5	$\frac{g\ COD\ m^{-3}\ _S}{g\ COD\ m^{-3}\ _X\ d^{-1}}$	(5)
$K_{IRB,bu}$	Half saturation constant of $X_{IRB,bu}$ for S_{bu}	200	$g\ COD\ m^{-3}$	(5)
$k_{IRB,pro}$	Maximum uptake rate of S_{pro} by $X_{IRB,pro}$	5	$\frac{g\ COD\ m^{-3}\ _S}{g\ COD\ m^{-3}\ _X\ d^{-1}}$	(5)
$K_{IRB,pro}$	Half saturation constant of $X_{IRB,pro}$ for S_{pro}	200	$g\ COD\ m^{-3}$	(5)

$k_{IRB,ac}$	Maximum uptake rate of S_{ac} by $X_{IRB,ac}$	5	$\frac{\text{g COD m}^{-3} \text{ _S}}{\text{g COD m}^{-3} \text{ _X d}^{-1}}$	(5)
$K_{IRB,ac}$	Half saturation constant of $X_{IRB,ac}$ for S_{ac}	200	g COD m^{-3}	(5)
$k_{IRB,h}$	Maximum uptake rate of S_h by $X_{IRB,h}$	5	$\frac{\text{g COD m}^{-3} \text{ _S}}{\text{g COD m}^{-3} \text{ _X d}^{-1}}$	(5)
$K_{IRB,h}$	Half saturation constant of $X_{IRB,h}$ for S_h	200	g COD m^{-3}	(5)
$K_{Fe^{3+}}$	Uptake affinity constant for Fe^{3+} by IRB	10	g Fe m^{-3}	(4)
k_{pre}	Precipitation rate	1	$\text{m}^3 \text{ g}^{-1} \text{ d}^{-1}$	(1)
$k_{dec,su}$	Decay rate coefficient of X_{su}	0.02	d^{-1}	(2)
$k_{dec,bu}$	Decay rate coefficient of X_{bu}	0.01	d^{-1}	(3)
$k_{dec,pro}$	Decay rate coefficient of X_{pro}	0.01	d^{-1}	(3)
$k_{dec,SRB,bu}$	Decay rate coefficient of $X_{SRB,bu}$	0.01	d^{-1}	(3)
$k_{dec,SRB,pro}$	Decay rate coefficient of $X_{SRB,pro}$	0.01	d^{-1}	(3)
$k_{dec,SRB,ac}$	Decay rate coefficient of $X_{SRB,ac}$	0.015	d^{-1}	(3)
$k_{dec,SRB,h}$	Decay rate coefficient of $X_{SRB,h}$	0.01	d^{-1}	(3)
$k_{dec,IRB}$	Decay rate coefficient of IRB	0.01	d^{-1}	(2)
f_1	stoichiometric parameters	0.13	—	(2)
f_2	stoichiometric parameters	0.27	—	(2)
f_3	stoichiometric parameters	0.41	—	(2)
f_4	stoichiometric parameters	0.19	—	(2)
f_5	stoichiometric parameters	0.2	—	(2)
f_6	stoichiometric parameters	0.8	—	(2)
f_7	stoichiometric parameters	0.57	—	(2)
f_8	stoichiometric parameters	0.43	—	(2)
η_1	stoichiometric parameters	1.65	—	(1)
η_2	stoichiometric parameters	2.82	—	(1)
Y_{su}	microorganism yield coefficient	0.1	g COD / g COD	(2)
Y_{bu}	microorganism yield coefficient	0.0366	g COD / g COD	(3)
Y_{pro}	microorganism yield coefficient	0.0366	g COD / g COD	(3)
$Y_{SRB,bu}$	microorganism yield coefficient	0.0329	g COD / g COD	(3)
$Y_{SRB,ac}$	microorganism yield coefficient	0.0329	g COD / g COD	(3)
$Y_{SRB,pro}$	microorganism yield coefficient	0.0342	g COD / g COD	(3)
$Y_{SRB,h}$	microorganism yield coefficient	0.0366	g COD / g COD	(3)
Y_{IRB}	microorganism yield coefficient	0.035	g COD / g COD	(4)

$K_{h2s, bu}$	Inhibition constant by H ₂ S on X_{bu}	276	$g\ S\ m^{-3}$	(3)
$K_{h2s, pro}$	Inhibition constant by H ₂ S on X_{pro}	276	$g\ S\ m^{-3}$	(3)
$K_{h2s, irb}$	Inhibition constant by H ₂ S on IRB	340	$g\ S\ m^{-3}$	(4)
$K_{h2s, srb, bu}$	Inhibition constant by H ₂ S on $X_{SRB, bu}$	256	$g\ S\ m^{-3}$	(3)
$K_{h2s, srb, pro}$	Inhibition constant by H ₂ S on $X_{SRB, pro}$	256	$g\ S\ m^{-3}$	(3)
$K_{h2s, srb, ac}$	Inhibition constant by H ₂ S on $X_{SRB, ac}$	244	$g\ S\ m^{-3}$	(3)
$K_{h2s, srb, h}$	Inhibition constant by H ₂ S on $X_{SRB, h}$	213	$g\ S\ m^{-3}$	(3)
C_{ac}	carbon content of acetate	0.0313	$mol\ g^{-1}\ COD$	(2)
C_{bio}	carbon content of biomass	0.0313	$mol\ g^{-1}\ COD$	(2)
C_{bu}	carbon content of butyrate	0.0250	$mol\ g^{-1}\ COD$	(2)
C_{pro}	carbon content of propionate	0.0268	$mol\ g^{-1}\ COD$	(2)
C_{su}	carbon content of sugar	0.0313	$mol\ g^{-1}\ COD$	(2)
C_{xc}	carbon content of decay	0.0279	$mol\ g^{-1}\ COD$	(2)
N_{bio}	Nitrogen content of biomass	0.00625	$mol\ N\ g^{-1}\ COD$	(2)
N_{xc}	Nitrogen content of decay	0.002	$mol\ N\ g^{-1}\ COD$	(2)

Source: (1) Gujer et al., 1999; (2) Bastone et al., 2002; (3) Fedorovich et al., 2003; (4) estimated in this work using experimental data; and (5) Somasundaram et al., 2009.

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