

Effect of Solvent on the Crystal Growth of One-Dimensional  
ZrO<sub>2</sub>-TiO<sub>2</sub> Nanostructures

Rahima A. Lucky<sup>1</sup>, Ruohong Sui,<sup>2</sup> John M. H. Lo,<sup>2</sup> and Paul A. Charpentier\*<sup>1</sup>

<sup>1</sup>Department of Chemical and Biochemical Engineering,  
University of Western Ontario, London, ON, Canada, N6A 5B9

<sup>2</sup>Presently at Department of Chemistry, the University of Calgary  
2500 University Drive, NW, Calgary, AB, Canada, T1N 1N4

**Table SI-1: Composition and weight loss at different stages of thermal analysis.**

Solvent	Stage 1		Stage 2		Stage 3		Total wt% loss
	T <sub>p1</sub> (°C)	Wt.(%)	T <sub>p2</sub> (°C)	Wt.(%)	T <sub>p3</sub> (°C)	Wt.(%)	
CO <sub>2</sub>	40	6.02	200	20.68	343	18.97	45.72
Hexane	75	6.31	198	19.29	333	22.02	47.92
Xylenes	86	5.61	191	38.04	425	13.54	59.01
Isopropanol	95	4.55	236	42.95	319	8.88	57.59
Ethanol	53	10.07	196	14.11	336	22.5	49.34

Note-a- composition of as prepared nanomaterials.

**Table SI-2. The thermodynamic properties and the average solubility parameters of the alkoxides.**

<b>Molecule</b>	$\Delta H_f^{0*}$ (liquid) Kcal/mol	$\Delta H_f^{0*}$ (gas) Kcal/mol	$\Delta H_v^{0*}$ Kcal/mol	$V^0$ (liquid) cm <sup>3</sup> /mol	$\delta$ (cal/cm <sup>3</sup> ) <sup>1/2</sup>
Ti(OPr <sup>i</sup> ) <sub>4</sub>	-377**	-360**	17	296***	7.44
Zr(OPr <sup>i</sup> ) <sub>4</sub>	-	-	31.5**	310***	9.99

Note: \*  $\Delta H_f^0$ ,  $\Delta H_v^0$  and  $V^0$  denote the standard formation enthalpy, the enthalpy change of vaporization and the molar volume of the liquid, respectively.

\*\* Ref. <sup>26</sup>

\*\*\* The molar volume was calculated from the density at 293 K. The liquid volume change was neglected for temperature changes from 293 to 298 K.

**Table SI-3. The related atomic and group contributions to the energy of vaporization and mole volume at 25 °C.<sup>33</sup>**

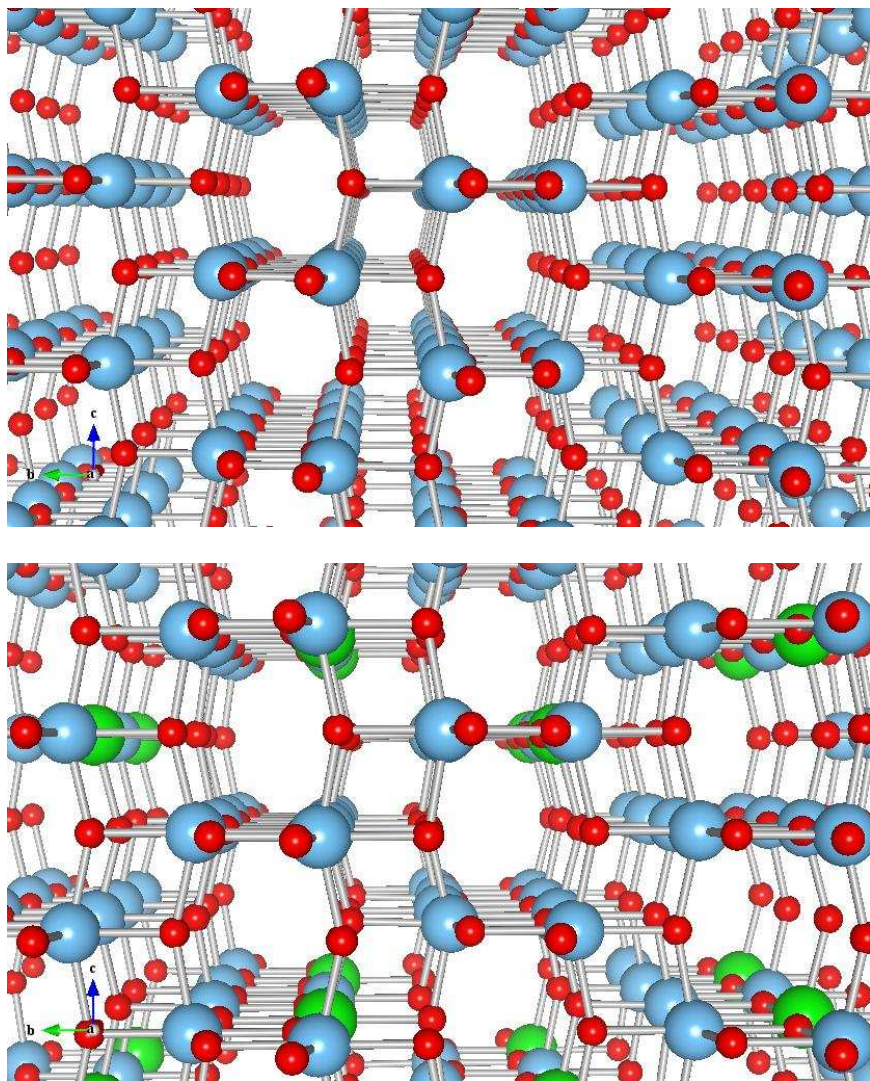
Atom or group	$\Delta e_i$ (cal/mol)	$\Delta v_i$ (cm <sup>3</sup> /mol)
CH <sub>3</sub>	1125	33.5
CH	820	-1.0
COO	4300	18.0
O	800	3.8
Zr (calculated by this work)	15400	30.8
Ti (calculated by this work)	930	16.8

\*- The solubility parameters of CO<sub>2</sub> are calculated for the selected temperature and pressure conditions using the density according to Giddings *et al.* with the provided values given in Table 2,<sup>21</sup>

$$\delta_{SC} = 1.25\sqrt{P_c} \frac{\rho_{R_{sc}}}{\rho_{RL}} = 0.384\rho \quad (\text{SI-1})$$

where,  $P_c$  is the critical pressure in atmospheres,  $\rho_{R_{sc}}$  is the reduced density of CO<sub>2</sub>,  $\rho_{RL} = 2.66$  is the reduced density of liquid CO<sub>2</sub> at its normal boiling point, and  $\rho$  is the density of CO<sub>2</sub> in mol/L.

**Figure SI-P1: The structures of DFT-optimized pure anatase (top) and Zr-doped anatase (bottom). Labels: Blue = Ti, Green = Zr, red = O.**



Lattice parameters (in conventional definition of lattice axes of anatase; different from those shown in the figures)

(1x2x1) TiO<sub>2</sub>: a = 3.80540 Å, b = 3.80549 Å, c = 9.47523 Å

(1x2x1) Zr-doped TiO<sub>2</sub>: a = 3.83552 Å, b = 3.83017 Å, c = 9.59331 Å

(2x2x1) TiO<sub>2</sub>: a = 3.80540 Å, b = 3.80549 Å, c = 9.47523 Å

(2x2x1) Zr-doped TiO<sub>2</sub>: a = 3.83618 Å, b = 3.83510 Å, c = 9.62817 Å

The Zr-doped anatase unit cell was generated by replacing one Ti atom by a Zr atom for every two unit cells of TiO<sub>2</sub>. This corresponds to the 12.5% of doping. In the (2x2x1) supercell, the two Zr atoms were placed such that the separation is farthest (the shortest Zr-Zr distance is 5.541 Å in the optimized (2x2x1) supercell of Zr-doped TiO<sub>2</sub>); this can eliminate the local, artificial distortion of the unit cell symmetry due to the Zr dopants.

### Details of the calculations of the (101) plane spacing of pure and Zr-doped anatase

The (101) plane spacing,  $d$ , can be deduced from the XRD spectrum using the Bragg's equation,  $d = (0.154 \text{ nm})/2 \sin \theta$ , where 0.154 nm is the wavelength of the X-ray source, and  $\theta$  is the diffraction angle. For pure  $\text{TiO}_2$  anatase,  $2\theta = 25.32^\circ$ , and thus  $d = 0.3513 \text{ nm}$ . In this work, we observed that  $2\theta = 25.17^\circ$  for Zr-doped anatase, and this corresponds to  $d = 0.3535 \text{ nm}$ . Hence, the percentage change in  $d$  is  $[(0.3535-0.3513)/0.3513] \times 100\% = 0.63\%$ .

By trigonometry, we can derive the (101) plane spacing of anatase (in Å) in terms of lattice constants:

$$d = |c| \sin \left( \tan^{-1} \left( \frac{|a|}{|c|} \right) \right) \quad (\text{SI-2})$$

Using the parameters given in figure SIP1, we can calculate the spacing for (1x2x1)  $\text{TiO}_2$ :

$$d = 9.47523 \sin \left( \tan^{-1} \left( \frac{3.80540}{9.47523} \right) \right) = 3.5313 \text{ \AA}$$

and for (1x2x1) Zr-doped  $\text{TiO}_2$ .

$$d = 0.95331 \sin \left( \tan^{-1} \left( \frac{3.83552}{9.59331} \right) \right) = 3.5571 \text{ \AA}$$

The resulting change in  $d$  is thus  $[(3.5571-3.5313)/3.5313] \times 100\% = 0.73\%$ . Similarly, we can calculate the  $d$  values for (2x2x1) pure anatase ( $d = 3.5313 \text{ \AA}$ ), Zr-doped anatase ( $d = 3.5628 \text{ \AA}$ ) and the corresponding deviation in  $d$  ( $\% \Delta d = 0.89\%$ ).