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**Algorithm 1:** SNC-SIMP for two objectives. The main passages of the algorithm are presented. The optimised points are generated iteratively by the MultiSimp function or by OptiStruct.

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// Generate the  $m$  reference points by solving the
// corresponding SOPs.
1 for  $j \leftarrow 1$  to  $m$  do
2    $\lfloor \{\mu_j\} \leftarrow j$ -th anchor point solution of SOP.
// Anchor points are normalised.
3  $\bar{\mu}_j = \frac{\mu_j - \min \mu_j}{\max \mu_j - \min \mu_j}$ 
4  $\bar{\mu} = \{\bar{\mu}_1, \dots, \bar{\mu}_m\}$ 
// Calculate utopia vectors.
5  $N_j = \bar{\mu}_j - \bar{\mu}_m$ 
// Assign PIT region parameters.
6  $a \leftarrow \{a_1, \dots, a_m\}$ 
7  $p = 0.4$ 
// Generate  $N$  evenly spaced approximation points
// associated to each anchor point.
8  $\alpha = \text{linspace}(0, 1, N)$ 
9  $\{U_i\} = \sum_{j=1}^m \alpha_i \bar{\mu}_j \quad \forall i = 1, \dots, N$ 
10 while  $\{U_i\}$  is not empty do
// Call SmartDistance function to calculate the smart
// distances between anchor points and approximation
// points and select the approximation point with the
// largest smart distance.
11  $\{s\} \leftarrow \text{SmartDistance}(\bar{\mu}, a, p)$ 
// Select the two approximation points adjacent to  $U_\ell$ .
12  $X_{p1} = U_{\ell-1}$ 
13  $X_{p2} = U_{\ell+1}$ 
// Call MultiSimp function to solve the SOP associated
// to the point  $U_\ell$  and subject to the additional normal
// constraints. The MultiSimp function is replaced
// with a call to OptiStruct for the case of the wing
// model.
14  $\{\mu_p\} = \text{MultiSimp}(N_j, \bar{\mu}, X_{p1}, X_{p2})$ 
15 if  $\mu_p$  is optimal then
16    $\lfloor \mu \leftarrow \{\mu, \mu_p\}$ 
// Remove the approximation point used at this
// iteration and restart.
17  $\{U_i\} \leftarrow (U_i \setminus U_\ell)$ 

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**Algorithm 2:** MultiSimp function to solve SOP subject to normal constraints. This pseudocode describes only the normal constraints associated to the bi-objective problem described in this work.

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**Input:**  $(N_j, \bar{\mu}, X_{p1}, X_{p2})$

**Output:**  $\mu_p, \bar{\mu}_p$

```
1 while  $change > tol \wedge iter < maxiter$  do
    // Calculate non-dimensional compliance  $\bar{C}$  and first
    // eigenfrequencies  $\bar{\omega}_1$ .
2    $\mu_p \leftarrow \{C, \omega_1\}$ ;
    // Update constraint vector.
3    $g(x) =$ 
     $(X_{p1}(2) - \bar{\omega}_1) + (\bar{C} - X_{p1}(1)), (\bar{\omega}_1 - X_{p2}(2)) + (X_{p2}(1) - \bar{C})$ ;
    // Call mmasub function. See relative documentation
    // for input arguments.
4    $x_{new} = mmasub(x, f, dfdx, g, dgdxdx)$ ;
5    $change = x - x_{new}$ 
```

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