SUPPLEMENTAL MATERIAL

COMPARISON OF CLIMBING-RIPPLE SETS

The evolution of the height of the climbing ripple set described in the main text, as well as the climbing ripple set immediately downstream (right-hand side of Fig. 1A), are compared in Fig. S1. For both ripple sets, the height increases from c. 8 mm to 22-23 mm and then decreases to 15-17 mm. This suggests that both ripple sets evolved from sandy ripples via large ripples to relict large ripples. Moreover, low-amplitude bed waves did not form, likely because of time constraints on ripple development and high suspended clay concentrations hindered evolution from large ripples to low-amplitude bed waves, as described in the main text. Figure S1 also reveals that the downstream climbing ripple set reached its maximum height over a shorter migration distance than the climbing ripple set described in the main text, but the steepest decrease in height occurred at a similar migration distance. This difference in the rate of development is inferred to result from the dynamic behavior of rippled beds; individual ripples affect the local flow field, which may either promote or hinder the migration rate and development rate of adjacent ripples (Baas, 1993). In this case, the climbing ripple set described in the main text may have promoted the development of large ripples in the climbing ripple set immediately downstream. Despite this difference in evolution, both climbing ripple sets are sufficiently similar to support the main conclusion that evidence for rapid flow transformation can be preserved in climbing ripple co-sets.

QUANTITATIVE EVIDENCE FOR RAPID AGGRADATION IN THE CLIMBING-RIPPLE SET

The angle of climb of climbing-ripple co-sets is controlled by the ratio of the suspended sediment fallout rate to the rate of downstream ripple migration. Although a steep angle of climb is more likely caused by a high aggradation rate (Sorby, 1859; Reineck, 1961; Allen, 1963; Walker, 1963; Jopling & Walker, 1968; Środoń, 1974; Banerjee, 1977; Jobe et al., 2012), Allen (1970) highlighted the main limitation of deducing physical sedimentary processes from climbing-ripple co-sets: “On the cautionary note, all that can be deduced from the geometrical properties of climbing-ripple cross-lamination is the ratio of the sediment deposition rate to the bedload transport rate”. In other words, high angles of climbing-ripple co-sets may be formed by any aggradation rate, provided that the ripple migration rate is significantly lower than the aggradation rate. For example, simple trigonometry can be used to show that a high climbing angle of 20° can be achieved at a low aggradation rate of 0.001 mm s⁻¹ by ripples that migrate at a low rate of 0.003 mm s⁻¹, or at a high aggradation rate of 0.1 mm s⁻¹ and with a high ripple migrate rate of 0.3 mm s⁻¹. In very fine sand, these two ripple migration rates are associated with either low flow velocities close to the threshold of sediment motion (c. 0.25 m s⁻¹) or high flow velocities near the transition to washed-out ripples and upper-stage plane bed conditions (c. 0.60 m s⁻¹), respectively (Baas et al., 2000). It is therefore essential to use other physical sedimentological parameters, in addition to angle of climb, to estimate the aggradation rate from...
climbing-ripple co-sets, and from this the duration of deposition represented by these co-sets. The main text of the present paper provides qualitative support for high aggradation rates. Herein, a complimentary more quantitative approach is outlined. It is assumed that the orientation of the climbing-ripple co-set is parallel to the paleoflow direction, as supported by a maximum foreset slope angle of 27°, which is close to the angle of repose for loose sand. This high slope angle also suggests that post-depositional compaction did not significantly influence the ripple height.

As discussed in the main text, the climbing-ripple set is divided into three sectors, representing a progressive change from turbulent flow (Sector 1), through turbulence-enhanced transitional flow and lower transitional plug flow (Sector 2), to upper transitional plug flow and quasi-laminar plug flow (Sector 3), with the transitional flow terms sensu Baas et al. (2009). Our quantitative assessment of aggradation rates and duration of deposition for each of these three sectors in the climbing-ripple set is given below, before estimating the total time needed to form the climbing-ripple set.

**Sector 1: Sandy current ripples formed by turbulent flow**

*Ripple development*

Sector 1 of the climbing-ripple set has an average climbing angle of 19.7°, with a ripple migration distance of 43.6 mm and an aggradation height of 15.6 mm. These sandy ripples grew in height from 8.5 mm to 12.9 mm between the base and top of Sector 1. The final height of 12.9 mm is below 14.9 mm, which, for the 0.124 mm sand observed herein, is the height at which the ripples are in equilibrium with the flow conditions, based on the ripple size predictor of Baas (1993):

\[ H_e = 3.4 \log_{10}(D_{50}) + 18 \quad (S1) \]

where \( H_e \) is the equilibrium height in millimeters and \( D_{50} \) is the median grain size in millimeters. It is therefore inferred that in Sector 1 the ripples did not reach equilibrium and evolved between non-equilibrium heights of 8.5 mm and 12.9 mm. Current ripples in 0.124 mm sand form at flow velocities between c. 0.25 m s\(^{-1}\) and 0.80 m s\(^{-1}\) in flow depths of more than 0.25 m (Southard & Boguchwal, 1990; their figure 3). Following the current ripple development model of Baas (1993) and interpolating between 0.095 mm sand (Baas, 1994) and 0.238 mm sand (Baas, 1999), ripples at these velocities need c. 2253 hours at 0.25 m s\(^{-1}\) and c. 6.6 minutes at 0.80 m s\(^{-1}\) to reach the observed final height of 12.9 mm. This large range in duration of deposition can be constrained in different ways, as detailed in the following sub-sections.

*Migration rate*

The ripple migration rates for flow velocities between 0.25 m s\(^{-1}\) and 0.80 m s\(^{-1}\), after conversion from Shields parameter to flow velocity and interpolation between 0.095 mm and 0.238 mm sand (Baas et al., 2000; their figure 1) range from 0.0037 mm s\(^{-1}\) to 2.18 mm s\(^{-1}\), respectively. These migration rates, at the migration distance of 43.6 mm in Sector 1, result in durations of deposition of between 0.3 minutes and 196 minutes. Hence, the time needed to deposit Sector 1 of the climbing-ripple set is reduced to 6.6 - 196 minutes.

*Transition from angular to sigmoidal foresets*

Ashley et al. (1982) found experimentally that the foreset laminae of sandy climbing ripples change from angular to sigmoidal, as the aggradation rate is increased from 0.0067 mm s\(^{-1}\) to 0.015 mm s\(^{-1}\). Since the cross-laminae in the climbing-ripple set are clearly sigmoidal (Fig. 1B), this
approach can be used to estimate the duration of deposition. At the aggradation height of 15.6 mm in the climbing-ripple set under consideration herein, these aggradation rates translate into durations of deposition of 38.8 minutes and 17.3 minutes, respectively. This suggests that this set was formed within 38.8 minutes, thus further constraining the duration of deposition to 6.6 - 38.8 minutes.

Turbidite duration estimation (TDURE) model

Baas et al. (2000) and Baas (2004) used the TDURE model to calculate the duration of deposition of sediment from the thickness of Ta, Tb and Tc divisions, and the height and angle of climb of climbing ripples in Bouma-type turbidites (Bouma, 1962). For the present case, TDURE yields a duration of deposition for Sector 1 of 1.2 minutes. However, this duration is a crude estimate, because TDURE assumes that: (i) the ripples start to form on an upper-stage plane bed; and (ii) the top of the climbing-ripple co-set represents slow flow at the threshold of sediment motion. Both of these conditions need not be representative of the sample studied herein. The base of the climbing ripple set may have formed at any velocity in the current ripple stability regime; lower initial velocities would increase the predicted duration of deposition of Sector 1. Moreover, the top of the set was probably formed at a velocity significantly above the threshold of sediment motion (c. 0.25 m s\(^{-1}\) for 0.124 mm sand), given that the ripples kept climbing steeply into Sector 2, which would decrease the predicted duration of deposition of Sector 1. Yet, the short duration predicted by TDURE, together with the above constraint of the duration of deposition to 6.6 - 38.8 minutes, renders it unlikely that the duration of deposition was longer than several tens of minutes.

Flow deceleration: the clay flow phase diagram

Given the muddy character of the deposits below, above and within the climbing-ripple co-set, we assume that the climbing ripples in Sector 1 were formed in a flow that carried cohesive clay. The velocity range at which current ripples form in 0.124 mm sand is linked to clay concentration through the clay flow phase diagram of Baas et al. (2009; Fig. S2). This diagram shows the stability regimes of turbulent, transitional and laminar clay flow as a function of flow velocity and suspended clay (kaolinite) concentration. Because the Sector 1 ripples formed in turbulent flow, the suspended clay concentration should have been below 4% (i.e. where 0.80 m s\(^{-1}\) crosses the boundary between turbulent flow [TF] and turbulence-enhanced transitional flow [TETF]), or at progressively lower maximum clay concentrations if the Sector 1 ripples formed below 0.80 m s\(^{-1}\), since the TF-TETF boundary shifts to lower clay concentrations as the velocity decreases. The yellow, red and purple arrows in Fig. S2 show three possible paths for the flow that formed the climbing-ripple set. The yellow arrow presumes that the flow decelerates, but the suspended concentration is constant (or weakly decreasing or increasing) during deceleration. This scenario is unlikely to explain the formation of the climbing-ripple set for two principal reasons: (i) the flow would be incapable of reaching upper-transitional plug flow or quasi-laminar plug flow behavior required to form Sector 3 of the climbing-ripple set before the velocity becomes too low for ripple migration at 0.25 m s\(^{-1}\); and (ii) a constant (or weakly decreasing or increasing) clay concentration is unlikely in waning flow and contrasts with the upward increase in clay content in the deposit. The red arrow represents a scenario in which the climbing-ripple set starts to form at a low velocity and then decelerates over a narrow range of velocities. This scenario requires a strong increase in clay concentration of almost two orders of magnitude to pass the various clay flow types needed to form all three sectors of the climbing-ripple set. This combination of weak flow waning and strong bulking of the flow with clay would be difficult to achieve without invoking specific external factors, such as tapping into an upstream clay source during development of the climbing-ripple co-set. A combination of deceleration over a wider range of velocity and a narrower range of clay concentration is a more plausible scenario (purple
arrow in Fig. S2), because a large decrease in velocity is often associated hydrodynamically with increased fallout of clay from suspension and thus an increase in clay concentration above the ripple crest and in the ripple trough. This scenario thus also explains the vertical increase in clay content in the climbing-ripple set. Moreover, the clay concentration does not need to increase over two orders of magnitude, as the clay concentration of the flow that formed the first ripple in Sector 1 of the climbing-ripple set may have carried up to 4% clay. Since a high initial velocity in the ripple regime is required to achieve the strong flow waning in this scenario, this increases the likelihood that the ripples in Sector 1 migrated rapidly and therefore the climbing ripple was exposed to rapid aggradation to maintain the climbing angle. In turn, this suggests that the duration of deposition of these sandy ripples was shorter than estimated with the above methods for determining flow velocity and ripple migration rate, because migration rate increases exponentially with flow velocity (Baas et al., 2000). For example, the above estimate of 6.6 - 196 minutes, based on maximum and minimum ripple migration rate, is reduced to 6.6 - 31.0 minutes and 6.6 - 7.8 minutes, if the climbing-ripple set was formed at Sector-1 averaged velocities of 0.35 m s\(^{-1}\) and 0.45 m s\(^{-1}\), respectively. These ranges are comparable to those inferred from the foreset laminae shape (Ashley et al., 1982) and the TDURE model (Baas, 2004) above.

_settling rate_

Jobe et al. (2012) used the following relationship between aggradation rate and particle fall velocity under hindered settling conditions for the analysis of climbing-ripple co-sets:

\[
ws_h \cdot Csusp = U_{bed} \cdot C_{bed}
\]  \(\text{(S2)}\)

where \(ws_h\) is the fall velocity corrected for hindered settling, \(C_{susp}\) is the concentration of sand or silt particles in the flow, \(U_{bed}\) is the bed aggradation rate, and \(C_{bed} = 0.65\) is the concentration of the sand or silt particles in the bed, assuming a random packing density. Values for \(ws_h\) were calculated from the hindered settling relationship of Richardson & Zaki (1954):

\[
w_{s,h} = w_s(1 - C_{susp})^{4.65}
\]  \(\text{(S3)}\)

where \(w_s\) is the fall velocity of a single particle in clear water. The fall velocity for 0.124 mm sand particles in clear water is 0.012 m s\(^{-1}\) (Soulsby, 1997). Combining Equations S2 and S3 and using a realistic range of \(C_{susp}\)-values for turbulent sediment gravity flows of 0.5% to 4% (cf. Fig. S2) yields 0.088 < \(U_{bed}\) < 0.60 mm s\(^{-1}\). For Sector 1 of the climbing-ripple set, this converts into a duration of deposition of between 0.4 minutes and 3.0 minutes. However, the fall velocity used herein may be overestimated, because the very fine sand particles did not settle through quiescent water, and thus turbulence in the flow will have reduced the fall velocity, and the presence of up to 4% clay will have further reduced the fall velocity through enhanced hindered settling and increasing the water viscosity. However, even if this reduction had been an order of magnitude, the duration of deposition of Sector 1 would have increased to only 4.3 - 29.5 minutes, well within the range of durations calculated with the above methods.

_summary for sector 1_

Although no precise values for the duration of deposition for the sandy ripples in Sector 1 of the climbing-ripple set can be calculated, the combination of methods used herein implies that Sector 1 was formed rapidly, within time periods of minutes to several tens of minutes.
Sector 2: Mixed sand–clay large ripples formed by turbulence-enhanced transitional flow and lower transitional plug flow

Sector 2 of the climbing-ripple set has an average angle of climb of 18.4°, with a ripple migration distance of 83.3 mm and an aggradation height of 27.7 mm. These heterolithic sand–clay ripples grew in height from 12.9 mm to 21.7 mm between the base and top of Sector 2. Two different approaches are taken herein to estimate the duration of deposition in the sub-sections below.

Comparison with experiments of Baas et al. (2011)

Large ripples in cohesive mixed sand–clay flows were described for the first time by Baas et al. (2011). The kinematic behavior of large ripples is more poorly known than that of the type of sandy ripples present in Sector 1, which have been studied for more than a century (e.g. Sorby 1859, 1908). Consequently, the duration of deposition of the large ripples in Sector 2 is more difficult to estimate than in Sector 1. Baas et al. (2011) described large ripples in heterolithic deposits of kaolinite clay and poorly sorted silty sand (median diameter: 0.084 mm). These large ripples formed at a mean flow velocity of 0.44 m s⁻¹, were up to 18 mm high and 203 mm long, and migrated at a rate that decreased from 0.236 mm s⁻¹ to 0.133 mm s⁻¹, as suspended clay concentration was increased from 1.1% to 8.0%. These numerical values are of the same order of magnitude as those inferred to predict durations of deposition, for the climbing ripple set examined herein, from the clay flow phase diagram of Baas et al. (2009) (e.g. purple arrow in Fig. S2). Applying migration rates of 0.133 mm s⁻¹ to 0.236 mm s⁻¹ to the climbing-ripple set in Sector 2 yields durations of deposition of 10.4 minutes and 5.9 minutes, respectively. These durations should be considered approximate, because the mean velocity at which the large ripples formed may not have been close to 0.44 m s⁻¹. A higher and lower mean velocity for Sector 2 would decrease and increase the duration of deposition, respectively.

Bed sediment flux and ripple height

Interestingly, the bed sediment flux associated with ripple migration is nearly constant (0.9 - 1.1 mm² s⁻¹) over almost the entire range of suspended clay concentrations (0.2 - 6.9%) at which ‘normal’ current ripples and large ripples were the stable bedform phase in the experiments of Baas et al. (2011; their figure 15c). Because the bed sediment flux is dependent on the product of ripple migration rate and ripple height, and ripple migration rate decreased as clay concentration was increased in the experiments of Baas et al. (2011), the bed sediment flux was governed primarily by the ripple height. Hence, an increase in ripple height in steady flow should result in a proportional decrease in ripple migration rate. If it is assumed that this relationship is applicable to other flow velocities and sediment sizes, and taking the conservative estimate of the Sector 1 duration of deposition of 6.6 - 38.8 minutes, Sector 2 could have been deposited in 21.2 - 125 minutes. This increase in duration reflects the increase in ripple height from 12.9 mm in Sector 1 to 21.7 mm in Sector 2, and the larger aggradation distance of Sector 2. However, these calculations do not include the possible contribution to the migration rate of the large ripples by fallout from suspension of clay particles, which make up more than half of the foreset laminae in Sector 2 (Fig. 1A,B), and that are also thicker than the clay-rich laminae shown in Baas et al. (2011). Incorporating this extra downward flux is expected to reduce the duration of deposition of Sector 2, but a precise reduction cannot be calculated at present.

Summary for Sector 2
We conclude that the two methods used herein suggest that several minutes to several tens of minutes were required to form Sector 2 of the climbing-ripple set. The rapid aggradation rate in Sector 1 thus continued into Sector 2.

**Sector 3: Clay-rich ripples formed by upper transitional plug flow and quasi-laminar plug flow**

Sector 3 of the climbing-ripple set has an average angle of climb of 44.2°, with a ripple migration distance of 22.2 mm and an aggradation height of 21.6 mm. The height of these clay-rich ripples decreases from 21.7 mm to 18.4 mm between the base and top of Sector 3. The duration of deposition of this section is estimated in two different ways detailed below.

*Bed sediment flux and ripple height*

As for the large ripples in Sector 2, a small amount of information is available from past work concerning the kinematics of clay-rich bedforms, which are interpreted to have formed by upper transitional plug flow and quasi-laminar plug flow in Sector 3 of the climbing-ripple set. Baas et al. (2011; their figure 11) measured the aggradation rate in the same rapidly decelerated kaolinite clay flows that formed the large ripples described above, but at higher suspended clay concentrations of 10.1% to 19.2%. In the first 15 minutes after flow deceleration, when the flow velocity was steady at 0.44 m s⁻¹, the mean aggradation rate ranged from 0.005 mm s⁻¹ to 0.023 mm s⁻¹. Using these aggradation rates, the 21.6 mm thick Sector 3 is predicted to have been deposited in 15.5 - 69.0 minutes. However, the aggradation rate at a fixed suspended clay concentration is expected to vary with flow velocity.

*Settling rate*

The settling velocity of clay particles is highly dependent on flocculation, but, owing to the low salinity of the water in the caldera lake, the clay may have aggregated into microflocs (Eisma, 1986), rather than staying as single clay particles that are rare in nature (Schieber et al., 2007), or forming larger macroflocs that are common in more saline water. The diameter of microflocs was delimited by Mikkelsen et al. (2006) to 0.036 - 0.133 mm, and the settling velocity of such microflocs is c. 0.126 mm s⁻¹ to 0.463 mm s⁻¹ (Fig. S4), which corresponds well with the mean settling velocity of 0.34 mm s⁻¹ for fresh-water flocs derived from eight major rivers (Lamb et al., 2020). These settling velocities were derived from the ‘model’ curve in Fig. S4, which denotes the relationship between the settling velocity for a single floc, \( w_s \), and floc diameter, \( D_f \) (Mehta, 2013):

\[
\frac{w_s}{\mu} = \frac{18\beta}{\alpha} \frac{\left( \rho_p - \rho_w \right) g}{\mu} \frac{D_p^{3-n_f}}{D_f^n} \frac{D_f^{n_f-1}}{1+0.15R_e^{0.687}}
\]

(S4)

where \( \alpha = \beta = 1 \) are particle shape factors, \( \rho_p \) is the density of the primary clay particle, \( \rho_w \) is the water density, \( \mu \) is the dynamic viscosity, \( D_p \) is the diameter of the primary clay particle, \( n_f \) is the fractal dimension of the floc, taken herein as 2 (Fig. S4; Mehta, 2013), \( R_e = \frac{w_s D_f}{\nu} \) is the floc Reynolds number, and \( \nu \) is the kinematic viscosity. Typical suspended clay concentrations for upper transitional plug flow and quasi-laminar plug flow within the expected range of flow velocities (Fig. S2) are between 5% and 10%, and thus well within the hindered settling regime. Using Equations S2 and S3, and following the same procedure as for the large ripples in Sector 2, estimated aggradation rates for the climbing ripples in Sector 3 are between 0.0077 mm s⁻¹ and 0.044 mm s⁻¹, which is equivalent to durations of deposition of 8.2 - 47.0 minutes.
Summary for Sector 3

The two methods used herein to estimate the duration of deposition of the mud-rich climbing ripples in Sector 3 both yield time periods of tens of minutes.

Conclusion

Our quantitative analysis of the climbing-ripple sets studied in this paper shows that the sandy ripples in Sector 1 and the heterolithic mixed sand–clay large ripples in Sector 2 formed within minutes to tens of minutes. The generation of the mud-rich ripples in Sector 3 may have needed somewhat longer, i.e. of the order of ten of minutes. We conclude that the entire climbing-ripple set was thus deposited within several tens of minutes. Such a duration supports the notion that the climbing-ripple set records rapid transformation from turbulent via turbulent-enhanced to a turbulence-attenuated sediment gravity flow.

References Cited


**Fig. S1.** Horizontal position of the ripple brinkpoint vs ripple height for two climbing ripple sets. Blue dots denote the climbing ripple set shown in Fig. 1. The open circles denote the downstream climbing ripple set (right-hand side of Fig. 1A).
Fig. S2. Clay flow phase diagram, showing the relationship between suspended clay concentration, for kaolinite clay, and depth-averaged flow velocity (modified after Baas et al., 2009). Turbulent, transitional and laminar flow types are highlighted by orange shadings. The blue dashed lines indicate boundary velocities between which current ripples form in very fine sand (Baas, 1993). The blue dot denotes the maximum kaolinite clay concentration at which current ripples can be generated in turbulent flow. Since kaolinite is a weakly cohesive clay mineral, this maximum concentration will be lower for other clay minerals, such as illite and bentonite (Baas et al., 2016). The gray dashed lines signify flow velocities of 0.35 m s\(^{-1}\) and 0.45 m s\(^{-1}\) used in the text. The yellow, red, and purple arrows indicate different flow paths for the flow that generated the climbing-ripple set, discussed in the text.
Fig. S3. Original (top) and interpreted (bottom) close-up photograph of backflow ripples on the lower slipface of the climbing ripples. See Fig. 1B for location.
Fig. S4. Functional relationship between the settling velocity, \( w_s \), and diameter of mud flocs, \( D_f \) (modified after Mehta, 2013). The gray area delimits the field data used to define the black curves (see Equation S4). The three curves use different fractal dimensions, \( n_f \). The present study uses \( n_f = 2.0 \). The blue dashed lines denote the limits of the size of microflocs in fresh water, according to Mikkelsen et al. (2006).