OPTIMIZING PROCEDURALLY GENERATED COOPERATIVE MULTIPLAYER GAME LEVELS

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ABSTRACT

Procedural level generation is a novel area of research within the field of computer graphics and game development. However, current research and implementations of procedural generation for cooperative games is sparse. Further study is required to validate the use of automatic level creation and to test additional methods of optimization for cooperative games. Additionally, despite many recent developments, many areas within the field of virtual reality remain underexplored. We propose a mathematically defined total cost function for controlling a procedural level generation algorithm for cooperative virtual reality games. This cost term controls an algorithm which gradually improves a generated solution over a series of iterations, bringing it to an optimal state. We present here two games with procedurally created levels and gameplay elements using this mathematical total cost function, as well as proposed experiments to validate the effectiveness of this content in encouraging cooperation and potential use cases for this technology.
CHAPTER 1. INTRODUCTION

1.1 Problem Statement

Procedural content generation (PCG) is an extremely versatile and up-and-coming area of research, particularly for companies in the entertainment gaming industry. It allows developers to automate many tasks and to semi-intelligently create large amounts of content quickly, thus saving a significant amount of time and resources. Procedural generation typically incorporates a stochastic process and can create game content at runtime, leading to infinite replayability in games which make use of it. The rogue-like genre of games is particularly keen to use random procedural generation to create an endless variation of game levels which are unique in each playthrough.

Several considerations must be taken into consideration by the developers during the creation of content generation algorithms. For example, the algorithm must be designed in such a way to ensure a consistent experience (e.g. a consistent level of difficulty) with each “solution” or “combination” of random elements. If done poorly, separate playthroughs can lead to vastly different levels of difficulty. In addition, developers must account for many potential “edge cases” which may cause a generated level or configuration to be unplayable or impossible to complete.

One area which is yet under-explored is tailoring procedural content generation algorithms in a way to encourage cooperation in a multiplayer game. Very few games handle cooperation in a way which truly encourages players to work together, instead simply having them act as identical (or near-identical) agents who act on their own. Two good examples of cooperative multiplayer games are Portal 2’s\(^1\) multiplayer mode and Overcooked\(^2\). In both cases, the game requires players to communicate with one another in order to complete a task.

Procedural content generation has immense potential to speed up the game development pipeline and to create unique content in each playthrough. However, due to factors such as the complexity of the issue, the high levels of creative and intuitive thinking to see its possible uses, and a

\(^1\) [https://store.steampowered.com/app/620/Portal_2/](https://store.steampowered.com/app/620/Portal_2/)
\(^2\) [https://store.steampowered.com/app/448510/Overcooked/](https://store.steampowered.com/app/448510/Overcooked/)
perceived lack of artist control over the generation process, many companies fail to utilize it to its full potential (if at all). This results in consistent but slow development times for hand-placed content which can greatly limit the size and scope of a game with a limited timeline. By making use of current procedural generation techniques, developers can significantly speed up their development pipeline and save artists/designers the tedious tasks of repetitively assembling similar levels.

1.2 Research Question

The following items represent the research questions for this study:

● To what degree can we control procedural level generation through a mathematical formula to effectively encourage cooperation
● To what degree are the levels of cooperation between two players in procedurally generated game levels similar to the degrees of cooperation between two players in manually created game levels?
● To what degree can this optimization algorithm ensure a fairly consistent level of required cooperation and difficulty across solutions?
● To what degree does playing procedurally generated cooperative game levels improve the cooperative behavior of individuals in performing cooperative tasks?

1.3 Research Significance

Procedural content generation holds immense potential for solving a wide variety of problems in a highly efficient manner. In addition to being incorporated into existing game companies workflows, procedural generation holds great potential for rapid development of virtual reality training software. Additional research must be performed to help verify the effectiveness and reliability of procedural generation to encourage its expanded usage in industry.

In addition to its applications in the field of entertainment video games, rapid generation of collaborative content has potential applications for the field of collaborative training. Whether for the purpose of creating games to teach team members to collaborate or to generate scenarios for safety/training simulators, these same generative systems can be applied to the developing field of serious gaming and VR training.
1.4 Purpose

The question which this research project intends to answer is as follows: to what degree can cooperative game levels be defined mathematically to procedurally generation game content. The results of the procedural content ideally should be user-tested and compared with a similar hand-assembled game level for validity. However, due to the COVID-19 pandemic and subsequent suspension of in-person user studies, this test was not able to be performed.

1.5 Assumptions

- Participants have some prior experience with video games
- Participants have some prior experience with virtual reality
- Participants should all be physically capable of interacting with virtual reality motion tracked controllers

1.6 Limitations

- Due to health concerns resulting from the COVID-19 outbreak, user studies were not able to be performed
- It may be difficult to accurately quantify the level of cooperation between two players
- Cooperation is a loosely defined concept and is highly situational and a user’s awareness
- Different participants may have different social behaviors and be more or less inclined to cooperation due to their personality

1.7 Delimitations

- Given the time constraints of the project, only two simple games will be developed to test the generation algorithm.
- The generation will be balanced with two players in mind.
1.8 Definitions

**Simulated Annealing:** an optimization algorithm used for finding an optimal (or close-to-optimal) solution to an optimization problem (Carr, 2012)

**Procedural Content Generation (PCG):** a method of automatically creating content (typically randomly) in a structured, algorithmic way rather than creating content manually or by hand.

**Virtual Reality:** a digital experience/simulation in which a user is immersed in a virtual environment

**Cooperative (co-op) Games:** a game in which two or more players must work together to accomplish a shared goal

1.9 Summary

This study aims to validate the usage of a total cost function for procedurally generating levels for a virtual reality cooperative game. Recent developments in procedural generation, the efficiency of random level generation to create vast amounts of replayable content, and the limitations of existing research in its applications for cooperative games necessitates further research to examine its potential effectiveness and use cases. This project proposes the usage of a mathematical total cost function to control a procedural generation system for creating cooperative VR game levels.
CHAPTER 2. LITERATURE REVIEW

2.1 Virtual Reality

Virtual reality is one of the most popular recent developments in technology in the field of game design. The emergence of consumer-affordable virtual reality equipment has created a boom in development and research. According to a Reuters article from 2018, “The Global Virtual Reality Market was valued at USD 3.13 billion in 2017 and is expected to reach USD 49.7 billion by 2023.” (Costello, 2018). According to a 2018 TrendForce study, total VR hardware sales have increased from 3.7 million to 5 million between 2017-2018 (Tsaj, 2018). Similar trends can be seen in the data from Forbes on monthly connected VR headsets as found through Steam (Rogers, 2019).

![Figure 1: Forbes data on monthly connected headsets on Steam](https://www.forbes.com/sites/solrogers/2019/06/21/2019-the-year-virtual-reality-gets-real/)

Market trends show a strong increase in virtual reality content, likely due to significantly reduced prices making the hardware affordable to consumers, coupled with the novelty of the relatively new technology. As compared to more traditional games or interactive digital media, immersive virtual reality has much greater room for future development and a larger untapped market potential. Industry developers and researchers alike must take advantage of the booming popularity of this technology in order to utilize it to its full potential.

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2.2 Virtual Reality Training

As virtual reality becomes more affordable and easily available to consumers and software developers, new and creative use cases for the technology are being found. Virtual reality offers an incredibly high level of immersion and a level of physical interaction/motion which traditional computer games/software lack, while being safe to use (Noguchi, 2019). This allows content creators to simulate potentially dangerous situations (such as construction job sites) without the risk of physical injury or to simulate tasks with large consequences for failure (such as performing surgery or flying planes) without risking damage to property of individuals (De Vries, et al. 204). Additionally, using virtual reality technology is a highly engaging and novel experience, often motivating greater levels of participation and focus which leads to long-term retention benefits. As a result, companies are becoming increasingly interested in virtual reality as an alternative to real-world or on-site training for applicable tasks.

In their 2013 paper, Farra et al. (Farra et al., 2013) discuss the potential for VR training for disaster response for nurses. When compared with a more traditional web-based method of instruction, the researchers found that virtual reality training resulted in significantly higher retention of the information over a 2 month period.

Virtual reality training, along with virtual reality in general, is becoming increasingly popular due to its many benefits. Given the importance of teamwork in many jobs (such for firefighters and the police), cooperative virtual reality training software could be greatly beneficial.

2.3 Cooperative Games

Cooperative games are a subcategory of multiplayer games in which two or more players must work cooperatively, typically against AI enemies or to solve puzzles (games with two or more teams against each other are usually regarded as competitive, even though they involve cooperation). Several different methods have been used throughout the history of video games to encourage (or even force) cooperative behavior between players. In their paper “Game Mechanics for Cooperative Games,” Rocha et al. lists some of the ways in which gameplay elements can be used to encourage cooperative behavior. Perhaps the most obvious of these is
“shared goals” in which cooperating players have similar (or identical) objectives which they need to complete, putting them on the same pathway to their goal. Two other similar design patterns mentioned are “complementary” and “synergies between abilities” which both involve asymmetry between the two (or more) players and their abilities. Creating differences between players is done to ensure that no one player can “do everything” and thus must rely on each other to make up for one’s own deficiencies (Rocha, 2008).

There are many other unique methods in which game mechanics can be used to force or encourage two players to cooperate in a video game. Some of these different methods are noted in a 2018 Gamasutra article by Thierry Lauret. Lauret defines four categories named “The Gate, The Comfort, The Class, and the Job” (Lauret, 2018). “The Gate” refers to cooperative mechanics which require both players to be present to complete a task (i.e. two players lifting a gate, hence the name). “The comfort,” however, “relies on having a challenge mechanic so incredibly hard that having more than one player is a necessity.” As compared to gate mechanics, comfort mechanics are theoretically possible but extremely difficult for a solo player to perform, thus strongly encouraging cooperative behavior rather than rigidly enforcing it. “The Class” and “The Job” both involve assigning different roles to each player, either through their player avatar or character (as in the class) or simply through player actions (as in the job). Similarly, in his 2011 Game Developers Conference (GDC) talk, Ubisoft’s Patrick Redding defines several cooperative “dynamics” which are mechanics to create cooperative behavior between two players. These are placed on a gradient of “prescriptive” (forced cooperation) to “voluntary” (encouraged but not required cooperation). These dynamics are “gating/tethering, exotic challenges, punitive systems, buffing systems, asymmetric abilities, combined abilities, survival/attrition” (Redding, 2011).

The options available for cooperation-inducing mechanics are many and designers have numerous options to choose from when designing such multiplayer games. The distinction between forced and voluntary cooperation (being somewhat of a gradient/spectrum rather than discrete states) is critical as well to define the degree of autonomy that players are allowed in a game and to define the minimum level of cooperation that is desired. More coercive methods can be utilized by developers/designers aiming to create an experience which is strictly multiplayer
(such as A Way Out⁴) while less coercive methods can be used to create a game in which multiplayer is strongly encouraged and implied but not rigidly enforced (such as with dungeons in World of Warcraft⁵).

2.4 Video Games’ Effects on Cooperative Behavior

The topic of the impact of video games on human psychology and behavior is quite broad, especially with regards to violent video games. One subset of this research area is the effect of games (either cooperative or competitive) on human cooperative behavior. A study by Greitemeyer and Cox aimed to examine this effect. The researchers defined two condition groups: one group of participants to play a game (Mario Kart: Double Dash⁶) in single player mode and another to player with a partner. Following this, the groups were separated and the participants were paired randomly with another participant (other than the one with which they had played previously). Participants were asked to complete a moral/trust dilemma with playing chips in which they were asked to give as many chips as they expected to receive from the other person. The study found that those who had played the cooperative mode experienced higher levels of trust than those who had played single player, even when paired with someone other than their original partner. (Greitemeyer & Cox, 2013).

2.5 Procedural Content Generation

Procedural content generation (PCG) is a popular new area of research as it allows developers to rapidly create large amounts of content without having to manually create them. This results in slower upfront development times as the procedural generation algorithms are developed and much quicker development speeds later as only fine-tuning needs to be made (Kruehl, 2017).

The history of procedural generation in games can be traced back many years to early pioneering games such as Rogue⁷. The original Rogue created a random dungeon for the player to explore and fight their way through and featured a perma-death (permanent-death) system in which a

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⁴ https://www.ea.com/games/a-way-out
⁵ https://worldofwarcraft.com/en-us/
⁶ https://www.mariowiki.com/Mario_Kart:_Double_Dash!!
⁷ https://docs.freebsd.org/44doc/usd/30.rogue/paper.pdf
player’s death was permanent and required a complete restart of the game. This game’s core concepts and namesake have spawned the genres “Rogue-Like” and “Rogue-Lite” which feature randomly generated content and frequently similar permadeath mechanics to the original.

![Figure 2: A screenshot of the game Rogue.](https://commons.wikimedia.org/wiki/File:Rogue_Screen_Shot_CAR.PNG)

Another well-known title which features heavy amounts of procedural generation is Minecraft, a sandbox exploration/crafting game and the current best-selling video game of all time⁹.

Procedural content can also be created by the developers and “baked” into static content, rather than being generated at runtime. In his talk at the 2012 SIGGRAPH conference, Caleb Howard of Electronic Arts explains how his team created 300 tracks for the snowboard racing game SSX, a feat which would have been impossible if done manually (Howard, 2012).

As the growing number of unique and interesting use cases shows, the potential applications for procedural content generation in the gaming industry are quite vast. A 2017 article by Jonas Freiknecht and Wolfgang Effelsberg (Freiknecht & Effelsberg, 2017) examined the various forms that procedural generation has taken in computer graphics as well as the prevalence of each type as found in either scholarly research or in industry. Some of the types of procedural content generation include: “creation of textures and materials, generation of floor plans, humanoid model generation, animation of humanoid models, and artificial personality generation” (Freiknecht & Effelsberg, 2017). One key takeaway from this study is the apparent

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⁸ Taken from [https://commons.wikimedia.org/wiki/File:Rogue_Screen_Shot_CAR.PNG](https://commons.wikimedia.org/wiki/File:Rogue_Screen_Shot_CAR.PNG)
⁹ [https://www.engadget.com/2019/05/17/minecraft-has-sold-176-million-copies-worldwide/](https://www.engadget.com/2019/05/17/minecraft-has-sold-176-million-copies-worldwide/)
divide between procedural content generation in research and in industry in some areas of procedural generation, suggesting a lack of communication between the two fields. This is the case with areas such as generating “stories and quests” which is more common in research, despite its obvious potential use cases. Additionally, the authors mention that “large companies are thrifty about how they model or automatically generate cities” (Freiknecht & Effelsberg, 2017). This shows that despite its increasing potential and the rise of popular procedural modeling software such as Houdini\textsuperscript{10}, companies can be slow to adopt procedural generation into their existing workflow. This issue is also mentioned by Luiz Kruel in his 2017 GDC talk on technical art and proceduralism. In this talk, he describes some of his experiences in his profession (as well as some colleagues’ experiences) in which artists, designers, and management are all slow and hesitant to adopt new methods of performing common tasks (Kruel, 2017). As with many industries, veterans in game development tend to become “stuck in a rut” and without exposure to newer, more innovative techniques, their workflow may remain inefficient and outdated.

There are many possible reasons why developers, especially large developers with well-established workflows, would not make use of procedural generation. As mentioned by Joel Couture in a Gamasutra article, procedural generation “can create stages that are too hard, stages that are too easy or plain dull, stages that feel like repeats of each other, or just otherwise create an array of flavorless or frustrating experiences.” (Couture, 2016). In addition, procedural content can impact the “flow” of the game due to a lack of direct designer influence and it is often difficult to tune a generation algorithm to adequately replicate this flow. Additionally, given the random element of content creation involved, games with procedural generation sacrifice the hand placement of game elements for faster and more varied content. This relinquishing of artist control can make developers feel uneasy and unsure over the consistency of the product which they will be delivering.

However, when done effectively and when sufficient consideration has been given to the possible edge cases, procedural content generation can be effective in creating game content without having it feel “bland” or “soulless.” While a few larger scale projects in recent years,

\textsuperscript{10} https://www.sidefx.com/products/houdini/
such as No Man’s Sky\textsuperscript{11} and Shadow of Mordor\textsuperscript{12} appear to show a widening acceptance of PCG. Additional research on procedural generation and its use cases are required to ease developer anxieties regarding the topic and encourage its expanded usage in the gaming industry.

2.6 Procedural Content Generation for Cooperative Games

Many of the well-known coop-supported procedural games (such as Minecraft\textsuperscript{13}, Don’t Starve\textsuperscript{14}, and No Man’s Sky\textsuperscript{15}) feature extensive single player modes as well and appear to have coop as an additional feature rather than a key element of the game. By comparison, many of the most iconic cooperative games (such as Overcooked\textsuperscript{16} and Portal 2\textsuperscript{17}’s multiplayer mode) feature manually created content.

Very little research has been done on the usage of procedural level generation in coop multiplayer games. One noteworthy article, “Procedural Content Generation for Cooperative Games” by Rafael Ramos stands alone in this area of study. In this study, the author aimed to examine the viability of using a procedural generation algorithm in a simple cooperative game (Geometry Friends) and whether or not users could determine which content was manually created and that which was automatically created. The results found that users believe all content to be made by hand and found strong levels of cooperation (even in levels which did not force cooperation). This study is a critical beginning for this area of research (Ramos, 2015). However, it has many limitations as mentioned by the author. Firstly, the generation algorithm used is not evolutionary, meaning it generates a random solution and checks its viability. If the level is unsuitable, a completely new solution is generated. By comparison, algorithms such as simulated annealing progress through a series of iterations and gradually bring a solution closer to an optimal state. Secondly, the scope of the game itself is quite small. All game levels are 2D and take place on a single screen (no scrolling maps). This limits the content being generated to a very small area. Additionally, the levels are fairly simple puzzles which require the users to

\textsuperscript{11} https://www.nomanssky.com/
\textsuperscript{12} https://store.steampowered.com/app/241930/Middleearth_Shadow_of_Mordor/
\textsuperscript{13} https://www.minecraft.net/en-us/
\textsuperscript{14} https://www.klei.com/games/dont-starve
\textsuperscript{15} https://www.nomanssky.com/
\textsuperscript{16} https://store.steampowered.com/app/448510/Overcooked/
\textsuperscript{17} https://store.steampowered.com/app/620/Portal_2/
cooperatively gather purple diamonds scattered about. The game features very few elements (players, diamonds, platforms, walls) and simple cooperative mechanics. In order to verify the usefulness of procedural generation for cooperative games, it must be applied to a wider array of games with different genres and form factors.

2.7 Simulated Annealing

Simulated annealing is a stochastic optimization technique for finding a solution to a computational problem through randomly generated solutions. It’s named is based on the classical blacksmithing where metal is heated to a high temperature for making large changes. As the material cools down over time, it becomes less malleable and changes become more precise. Similarly, with simulated annealing, a series of optimization iterations will start with a high temperature value which allows for a wide range of values to be accepted during each proposed change to the solution, including potentially “bad” changes which take the solution farther from a desired outcome. As the iterations progress and the temperature cools down, the changes become less drastic until, ultimately, a final solution is reached which meets the desired conditions (Carr, 2012). During each iteration, a “move” is performed: an action in which the current configuration or solution is altered slightly in a random way. Depending on the desired results and the content being optimized, developers can define any number of moves to be a part of their optimization process.

In the paper “Make it Home: Automatic Optimization of Furniture Arrangement” explored the use of simulated annealing as part of an algorithm to generate random arrangements of furniture (Yu, et al. 2011). The generation algorithm determines things such as pairwise relationships between objects (such as between tables and chairs) and required visibility (such as between a sofa and a tv) by providing examples of hand-placed furniture arrangements. Based on these pairwise relationships, several cost terms are defined for the simulated annealing process. Less accurate arrangements lead to higher costs which the optimization then tries to correct. During each iteration, a random move of objects occurs. Then, the system re-assesses the current cost. This cycle continues as the furniture arrangement becomes more optimal, ultimately resembling a sensible configuration. The key factor which allows simulating annealing to be effective for solving this problem is that the relationships between objects can be mathematically defined and
therefore optimized using cost terms. For instance, if a chair is very far away from its corresponding table, the system knows to correct this by gradually moving the chair towards the table (or vice versa), thus reducing the cost.

Another study conducted by Zhang, et al. in 2019 used simulated annealing to create a virtual exercise game which can easily alter the difficulty (Zhang, et al. 2019). The game is similar to preexisting dance games in which the user must perform a sequence of poses, one after the other. The researchers used a Microsoft Kinect to capture full-body movements for gameplay. A series of 10 movements were defined and the 100 different transitions between these poses were measured for difficulty. Based on the difficulty of moving from one pose to another, the generation algorithm is able to create sequences of poses for the player which have a fairly uniform difficulty. A similar study, also in the vein of virtual reality exercise games, examined the use of simulated annealing to generate optimized game levels of a user-specified difficulty by formulating the game level design problem to a total cost function. One feature of this study is that the generation system uses a series of predefined “chunks” which are assembled together randomly to create the final level. (Xie, et al. 2018).

Simulated annealing is shown to be an effective means for generating solutions to complex problems. Additionally, it allows a developer to mathematically define terms by which to perform an optimization. It allows for solving complex problems and, as can be seen from the various applications, it readily applied to many complex issues.
CHAPTER 3. METHODOLOGY

3.1 Development

The primary development tool for this project is the Unity 3D Game Engine. Models and other assets were primarily acquired through the Unity Asset Store. A list of assets used in this project is included below:

- Photon Unity Networking\(^\text{18}\) (networking scripts)
- Polygon Dungeons\(^\text{19}\) (fantasy dungeon 3D models)
- Polygon City\(^\text{20}\) (city 3D models)
- Epic Toon FX\(^\text{21}\) (cartoony VFX)
- An HDRI Image from HDRI Haven\(^\text{22}\) (a skybox)
- Steam VR\(^\text{23}\) (the VR framework for the project)

The game is developed in Unity using the Steam VR framework. This framework contains many scripts to rapidly develop virtual reality projects and can be targeted to many different platforms, including Vive, Oculus, and Windows Mixed Reality. The project was primarily targeted for the HTC Vive Headset and testing was performed on a Windows Mixed Reality Headset (Samsung Odyssey).

Input for the two games varied. For the thief chasing game, a keyboard was used, while for the dungeon RPG game, two motion-tracked VR controllers were used. Likewise, the thief chasing game was designed to be played while seated while the dungeon crawl game was designed to be played while standing.

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\(^{19}\) [https://assetstore.unity.com/packages/3d/environments/dungeons/polygon-dungeons-pack-102677](https://assetstore.unity.com/packages/3d/environments/dungeons/polygon-dungeons-pack-102677)


\(^{21}\) [https://assetstore.unity.com/packages/vfx/particles/epic-toon-fx-57772](https://assetstore.unity.com/packages/vfx/particles/epic-toon-fx-57772)

\(^{22}\) [https://hdrihaven.com/hdris/](https://hdrihaven.com/hdris/)

\(^{23}\) [https://assetstore.unity.com/packages/tools/integration/steamvr-plugin-32647](https://assetstore.unity.com/packages/tools/integration/steamvr-plugin-32647)
In the initial stages of development, it was also planned to use the Virtuex Omni for movement. However, due to the closure of campus due to health concerns, this was not feasible. Rather, for the dungeon game, a gesture based movement system was employed.

3.2 Games

In order to test the algorithm and its effectiveness in encouraging cooperation, two games were developed. The first game is a simple game in which the two players control police/law enforcement officers who must locate and apprehend a criminal running through a city. The users need to work together to corner and apprehend the thief. The second game is a fantasy dungeon crawl game, somewhat in the vein of the original rogue game (a pioneer of procedural content in games). The users are required to navigate through the dungeon, fighting various enemies, solving puzzles, and ultimately locating various keys to open the door to the exit. These two games are described in further detail below.

3.3 Game 1: Criminal Chase

The first game developed with the simulated annealing procedural generation algorithm is a thief chase game. In this game, players would control two police officers in cars. They will be instructed to chase down a criminal in a red sports car who will be driving around the city in an attempt to evade the officers. If players get within a close distance of the criminal (~5 meters), the criminal will have been successfully caught, thus ending the game and prompting a victory message. The players each have a map which allows them to see the location of themselves and the other player so that they can coordinate with one another.

![Figure 3: An Example Level Layout of the Criminal Chase Game](image)
Figure 4: An Screenshot of a First Person View from Within the Police Car

The optimized parameters for this game include the following:

- The enemy speed
- The enemy detection radius
- The traffic density
- The starting distance between the players
- The navigation difficulty of the level (based on the number of streets)
- The speed of traffic light changes

These cooperative parameters are designed in a way to create variations in how the players must collaborate. For example, in a configuration with a fast thief but minimal traffic, players must collaborate to try to corner the player since one player would not be fast enough to catch them.
3.4 Game 2: Dungeon Delver

The second game developed is a fantasy RPG dungeon crawler game. In this game, players will be instructed to collect a certain number of keys scattered throughout the generated dungeon in order to unlock a door and escape the dungeon.
Movement in this game uses gesture based controls to reduce motion-sickness. To move around, users hold down the trackpad on either or both controllers (a button typically used for movement or teleportation in VR), and then swing their arms in the reverse direction that they wish to move (i.e. swing arms backwards to move forwards). This motion simulates the real-world motion of the arms when walking/running and is sometimes referred to as “rowing.” The players are unable to jump and their vertical motion is controlled only by gravity.

The optimized parameters for this game include the following:

- The number of rooms
- The number of traps/hazards
- The number of enemies
- The number of required keys
- The starting health of player
- The likelihood of a torch being lit by default

This game has slightly different cooperative elements due to asymmetrical player roles. One optimization parameter is the chance for a torch in a room to be lit at the start of the game. There is one grabbable torch which the players can use to light other torches in the scene to illuminate their path. Fewer lit torches is a result of higher target cooperation values. Traps and hazards often contain “cooperation-suggestive” elements which become significantly more difficult when done alone. A list of these traps/hazards is given below:

Table 1: A list of hazards for the dungeon crawler game

<table>
<thead>
<tr>
<th>Crates</th>
<th>Must be pushed out of the way, are easier/quicker to push with more players cooperating</th>
</tr>
</thead>
<tbody>
<tr>
<td>Stone Doors</td>
<td>Doors with switches, one player can stand on a switch, players can run through themselves if quick enough</td>
</tr>
<tr>
<td>Stuck Door</td>
<td>Doors which can only be broken by the warrior character</td>
</tr>
<tr>
<td>Locked Door</td>
<td>Doors which can only be unlocked by the mage character</td>
</tr>
<tr>
<td>Claptraps</td>
<td>Traps a player temporarily, preventing them from moving</td>
</tr>
<tr>
<td>Pendulum</td>
<td>Deals damage to a player when hit</td>
</tr>
</tbody>
</table>

This game features several patches used in its procedural generation which are divided into two categories: rooms and hallways. The game begins with a fixed starting room from which to build. When a new room or hallway is being added, a random door of the new patch is snapped to a random available door (a door in a patch already in the level which does not have another patch connected to it). Following this, the system performs a quick check using the bounding boxes of all the patches in the scene to check for overlap, in which case the new room would be discarded regardless of whether or not the addition of the room improved the current solution. Below are some in-editor screenshots of the different patches.
The main adjustable parameter of the optimization algorithm is the target cooperation value. This value is intended to control the degree of cooperation by adjusting the amount and intensity of several level elements and gameplay parameters.

When the optimization begins, the cost will be very high due to the initial emptiness of the scene and the lack of cooperative elements in it. As the optimization progresses, random moves will begin to place gameplay elements and adjust parameters until the level matches closely the desired cooperation level, thus decreasing the cost to near zero. This setup allows certain configurations to rely on different gameplay elements in order to encourage cooperation than other configurations. For example, one generated level for the city game may have a fast enemy with minimal traffic and pedestrians whereas in another level the inverse may be true. This
allows for a diverse array of levels to be generated with different challenges to face across configurations.

3.6 Cost Terms

The cost term comprises the core of the optimization algorithm. Cost here is defined as the “distance” between the current solution and a desired solution. Higher costs penalize the algorithm into making decisions to reduce the cost, thus dissuading it from making sub-optimal changes resulting in poor content.

The total cost function ($C_{Total}$) will feature two main cost terms ($C$) which each break down into more subterms. These are detailed below:

- Level Cost Term ($C_L$)
  - Adjacent Chunk Variation Cost ($C_V$)
  - Level Size Cost ($C_{LS}$)
- Game Cost Term ($C_G$)
  - Players ($C_P$)
  - Enemies ($C_E$)
  - Items ($C_I$)
  - Environment Hazards ($C_{H}$)

The Level Cost Term controls the foundational level structure, such as the placement of building patches. This is separated from the target cooperation value in order to ensure levels are of a consistent size/content amount. The Game Cost Term is controlled by the target cooperation value. A higher desired cooperation would require more cooperative elements (such as more difficult enemies or more hazards).

Each cost term is assigned a certain weight ($W$) to which it is multiplied. This value is user-defined and is used to increase or decrease the influence of a particular cost term. The total cost of the entire optimization solution is calculated from the sum of these two costs multiplied by
their respective weights. Depending on which game is being played, these cost terms will affect
different parts of the generated level and its contents. For example, the “level layout” parameter
in the criminal chasing game will alter the placement of city buildings and streets whereas in the
dungeon crawler RPG it will place the adjacent dungeon rooms.

The Game Cost Term is controlled by the amount of desired cooperation between the two
players.

Some game elements feature discrete elements (such as rooms) which feature a fixed value
associated with them. As rooms are added, their values are summed together to find the total
contribution of all rooms in the scene. The same concept applies for elements such as enemies in
which the total value of enemies is the sum of the value of each enemy.

The game cost ($C_G$) is formulated using the following equations:

$$C_{COOP} = | V_{COOP} - T_{COOP} |$$

$$V_{COOP} = W_P V_P + W_E V_E + W_I V_I + W_H V_H$$

where:

$$V_{P,E,I,H} = f(V_{Min}, V_{Max}, V_{Current})$$

The layout cost ($C_L$) is formulated using the following equation:

$$C_L = W_{LP}|V_{LP} - T_{LP}| + W_V C_V$$

Firstly, a target cooperation value ($T_{COOP}$) is specified by the user. The Cooperation cost ($C_{COOP}$)
is defined as the distance from the current cooperation value ($V_{COOP}$) calculated from the current
configuration and the target cooperation value. The current cooperation value ($V_{COOP}$) is
calculated from the sum of each of the four cooperation elements with their respective weights
($P$=Players, $E$=Enemies, $I$=Items, $H$=Hazards). Each of these values is defined by an inverse
linear interpolation function ($f$). Due to the usage of an inverse linear interpolation (inverse lerp),
all the values are normalized to the range of 0.0 and 1.0. Minimum difficulty ($V_{Min}$) and
maximum difficulty ($V_{Max}$) values are defined and the current values of a parameter ($V_{Current}$). For
example, the player optimization value ($V_P$) is calculated using the current distance between the
players by inverse interpolating this value between the minimum required cooperation player
distance and the maximum required cooperation player distance.

The level layout cost term is handled separately from the cooperative gameplay elements and is
defined by the cost term $C_L$. $V_{LP}$ and $T_{LP}$ refer to the current value of the level patches and the
desired value for level patches, respectively. $CV$ is the variation cost, a unique cost term
(calculated differently for different games) which is used to disincentivize the generation
algorithm from placing many of the same patches and attempts to alternatively create a diverse
and varied solution.

The individual cost of elements (such as enemy cost $C_E$ for example) will be calculated based on
which game is currently being played. One example would be an “enemy” optimization move in
the RPG game. The total value of the enemies would be determined by factors such as the
number of enemies and their difficulty. An example of this is the room placement cost term
equation as provided below. The current cost of the room optimization is defined as the distance
between the sum of the current room values (based on the number of rooms and their sizes) from
the desired total value.

$$C_{LP} = \sum_i \| R_i^2 - R_i \|$$

$$C_T = C_L + C_{coop}$$

where $R$ denotes the desired room configuration, $R \in \{R_i, \text{where } i=1,...,N\}$ and $R_2$ denotes the
new room configuration.

Similar calculations will be performed for the additional cost term elements. Some additional
examples of these cost terms and their implementations in the two games are detailed in the
diagram below.
This optimization algorithm can be readily applied to numerous other game types which feature similar elements (level, environment hazards, players, items, enemies).

### 3.7 Optimization

The optimization begins by generating a random starting condition, depending on the game chosen. For the dungeon game, the starting condition is a starting room, from which the optimization algorithm branches off of. For the city chasing game, the starting condition is a city with completely random patches and default parameters for all variables. Then, it proceeds through a number of iterations and checks (in the proposed case, one iteration/move per frame). During an iteration, the system first decides which type of change to perform (called a “move”). The types of moves are detailed in the section below (3.8). Once a type of move has been randomly chosen, a random change to the scene is proposed. For example, for a level layout move, the system could add or remove a room from the level. The cost ($C_p$) of the proposed alteration is computed and compared to the cost of the current configuration ($C_c$). If the cost
of the proposed configuration is less than that of the current configuration (meaning the proposed solution is closer to an optimal solution), the proposed change is accepted and the changes to the level are made (such as actually adding the in-game object for a proposed room). However, if the solution is less optimal/has a higher cost, the algorithm has a probability \( p \) of accepting depending on the cost difference \( D \) and temperature \( t \) as defined by the function below:

\[
p(C_C \lor C_p) = \exp\left(\frac{-1}{t} D\right) < R(0,1)
\]

where:

\[
D = C_C - C_p
\]

\( R(0,1) \) is a random floating point number between zero and one. When the optimization first begins, due to the high temperature, the probability of accepting “bad” moves is quite high. As the iterations continue, the temperature “cools down” as the solution becomes closer to its final configuration.

In this equation, the value \( t \) refers to the current optimization temperature. As with the metallurgical process which the simulated annealing process is named for, the optimization begins with a very high temperature which lowers as the optimization progresses. While this can be done gradually (i.e. linearly decreasing the temperature each iteration from max temperature to zero), in this project, we lower the temperature in three fixed intervals. This temperature impacts the optimization in multiple ways. First and foremost, as can be seen from the above equation, a higher temperature results in a higher chance of a “bad” move being accepted. Secondly, during the different temperature intervals, we prioritize certain moves (i.e. we prioritize more drastic moves such as add/replace room during high temperatures with more gradual/fine moves being for lower temperatures). Both of these result in the optimization exploring a wider range of variations earlier on while gradually refining to a final configuration (as with metal smithing).

### 3.8 Optimization Moves

Each iteration of the optimization process results in a random change, called a “move” being proposed. This random move may or not be accepted depending on whether or not it is a
beneficial move and what the current temperature of the optimization is. Each random move consists of a small change to the current optimization configuration/solution. Some of the options for moves may take the solution in opposite directions. For example, there can exist moves for a room based game generation to add a room or to remove a room.

When a move is proposed, before the actual changes are made in the scene (i.e. before a room is added), the costs of the current solution and the proposed solution are calculated. For instance, the current solution could contain the values of 3 different rooms while the proposed room contains 4 different rooms, the cost being the difference between the room value and the ideal room value. If the cost of the proposed solution is lower than the cost of the current solution, this signifies that the proposed change is beneficial and the change is accepted. If the change is not beneficial (if proposed cost ≥ current cost), the algorithm will accept or reject based on the acceptance function defined in the previous section (3.8 optimization).

Only after the change has been accepted will the changes be made in the scene. In the case of adding a room, at this stage the new room game object/prefab is actually instantiated into the level and placed in the correct position, linked to an existing room by a doorway. It is in this place that certain move-specific checks will be performed. When a room is being added, physics overlap checks are used to check whether or not the new room would overlap an existing room.

Table 2: An example list of moves of the RPG dungeon game, divided into the 5 main categories of moves

<table>
<thead>
<tr>
<th>Level</th>
<th>Player</th>
<th>Item</th>
<th>Environment</th>
<th>Enemy</th>
</tr>
</thead>
<tbody>
<tr>
<td>Add Room</td>
<td>Move Player Spawn</td>
<td>Add Key</td>
<td>Add Lit Torch</td>
<td>Add Enemy</td>
</tr>
<tr>
<td>Remove Room</td>
<td>Increase Player Health</td>
<td>Remove Key</td>
<td>Remove Lit Torch</td>
<td>Remove Enemy</td>
</tr>
<tr>
<td>Move Room</td>
<td>Decrease Player Health</td>
<td>Add Chest</td>
<td>Add Trap</td>
<td>Swap Enemy</td>
</tr>
<tr>
<td>Swap Rooms</td>
<td></td>
<td>Remove Chest</td>
<td>Remove Trap</td>
<td>Increase Enemy Detect Radius</td>
</tr>
<tr>
<td>Replace Room</td>
<td></td>
<td></td>
<td></td>
<td>Decrease Enemy Detect Radius</td>
</tr>
</tbody>
</table>
3.9 Stopping Condition

There are multiple methods of determining when the optimization should halt. First and foremost, a maximum number of possible iterations should be set which will stop the optimization when reached. Additionally, when the optimization begins to approach an “acceptable” cost (where $C_T$ approaches 0), the moves will result in minimal to no positive changes. If it is detected that no changes have been made over the last several hundred iterations, the current solution can be regarded as the ideal solution and the optimization can stop. The number of iterations to wait prior to stopping is user defined and depends on the complexity of the problem being solved.
3.10 Code Diagrams and Pseudocode

Figure 12 Flowchart of the optimization logic.
//this function is the main function which calls a iteration
of the generation algorithm

optimization step:
    if optimization has begun and is not terminated
        choose random move
        switch on random move
            case level move
                propose random level move
            case environment move
                propose random environment move
            case player move
                propose player environment move
            case item move
                propose random environment move
            case enemy move
                propose random environment move
        
        if iteration<=500
            temperature = 100
        if iteration>500
            temperature = 50
        if iteration>1000
            temperature = 25

    if current iteration > max iterations or if insignfigant
change in last 100 iterations
        terminate optimization

Figure 13: Pseudocode of the main iteration loop, the random move picking, and the stop condition
Figure 14: Pseudocode of a level move for the dungeon game

```plaintext
//this function is an example function to choose a move for a level term
propose random level move:
    choose random level move
    switch on random level move
        case add room
            propose add room
        case remove room
            propose remove room
        case replace room
            propose replace room
        case swap room
            propose swap room
```

Figure 15: Pseudocode of an example move (propose adding a room)

```plaintext
//the function is an example propose move function for adding a room
propose add room:
    choose random room patch
    calculate current room value
    calculate proposed room value with random room patch
    if move check with current and proposed values
        add random room patch to scene
```

Figure 16: Pseudocode of the move check equation

```plaintext
//the function is the probability acceptance function for moves which would increase the cost
move check:
    calculate current total cost
    calculate proposed total cost
    if proposed total cost < current total cost
        accept move
    else
        delta = difference between propose total cost and current total cost
        probability to accept = e^-delta/temperature
        if random(0.0,1.0) < probability to accept
            accept
        else
            reject
```
3.11 Example Results

Based on this simulated annealing algorithm, here are some example layouts of levels in the current prototype. Increasing the total value (as seen in the second set of images) leads to more rooms being placed into the scene. A user-defined target total value can be adjusted to control this. A higher target coop value results in a higher initial cost, resulting in moves adding value to the scene in the form of additional rooms to reduce the cost (with the total cost being the difference between the current value and optimal value). Likewise, increases in the ideal value for the “coop” cost term could result in more enemies being placed.

Figure 17: Some example dungeon layouts from the prototype (Total Room Value=50).

Figure 18: Some example dungeon layouts from the prototype (Total Room Value=100).

In order to test the patterns of the simulated annealing algorithm and its changes to the game level, we can plot the total cost of the level as it progresses through the iterations. Some examples of this are shown below, along with screenshots of the corresponding game level. One key element of the simulated annealing process is that it will occasionally accept a suboptimal response (at the points where the trend line goes up rather than down) in order to overcome a
local minimum. However, the likelihood to accept a bad move decreases as the iterations progress and the temperature is cooled.

Figure 19: Some examples of the prototype optimization iterations along with in-game screenshots of the results.

3.12 Specific Overrides

The simulated annealing algorithm works well to ensure varied configurations by examining a wide range of possible solutions and using its decreasing temperature. However, there are several instances where this system of proposing moves and accepting or rejecting based on costs must be circumvented. For instance, in the case of a game where players must acquire a certain number of items to complete their task (as in the dungeon RPG game), care must be taken to ensure that enough of these are spawned in each solution. In this case, a more direct method must be used, circumventing the typical system of suggesting change and discouraging bad moves. All potential edge cases must be considered to prevent uncompletable solutions.
CHAPTER 4. PROBLEM FORMULATION

4.1 Objectives

This study aims to examine the validity of procedural content generation for levels in cooperative games.

4.2 Proposed Testing Methodology

The cooperative level generation algorithm can be used in multiple potential experiments. Here, we propose two different experiments. Given health concerns and the recent decision of the IRB to suspend all in-person user studies, coupled with the nature of this project as a virtual reality project (with VR headsets being difficult to sanitize properly), these experiments are not currently able to be conducted. They are proposed here as potential areas of research.

Firstly, we propose an experiment to analyze the effects of the “target cooperation” variable and its impacts on the resulting levels of cooperation among the players. To test this, a study would be conducted of at least 16 groups of two players, with analysis being conducted across these 16 groups. Each player group would play both games with procedurally generated levels with target cooperation values of low, medium, and high. Following playing each of these, the participants would complete a brief questionnaire (included as an appendix). More information on this questionnaire can be found in section 4.2. In addition to the data from this survey, additional logged data will be used (please see section 4.3). Corrections will be made to account for the increased level of familiarity with the game as they have played more successive levels. We hypothesize that the target cooperation parameter will strongly correlate to the levels of cooperation experienced by the participants as they play the games.

Secondly, we propose an experiment to analyze the effectiveness of playing procedurally generated cooperative game levels on cooperation between two individuals.
4.3 Validation Questionnaire

A questionnaire for the proposed experiment can be used to gauge the level of cooperation between two users. This questionnaire is included as Appendix A.

4.4 Data Logging

During the experiment, some quantitative data will be logged based on the players’ experience. This data comes in various forms and contains mostly quantitative data. The following are the pieces of data which will be logged:

- How long it took the players to complete the level
- The number of dialogue interactions over voice chat between the two players
- The distance of the two players to one another (logged 4 times/second)

4.5 Testing Networking

The Unity network package Photon will be used to facilitate networked functionality between the two locations. Additionally, a common network solution will need to be found allowing the two machines to connect. This may involve processes such as acquiring a router separate from the campuses main network (to bypass restrictive firewalls) or using a pass-through app such as Hamachi. A software such as Discord or Skype will be used to transmit voice between the two players.

Given the time constraint of the project, before playing, the procedurally generated levels are “baked” by saving the level configuration to a static scene. This is done in order to prevent the data from the level configuration resulting from the procedural generation (such as the room/level layout and all the optimized parameters) from needing to be synced over the network. Having the levels be generated at runtime rather than generating them ahead of time and saving them would require a large amount of data to be synced across the network, causing lag and possibly the loss of data. This method also has the additional benefit of allowing the navigation mesh (navmesh) to be baked without needing to worry about runtime baking.
The ideal solution to this issue would be to generate the level on one client machine (likely the host machine) and have the optimized level data be transmitted only one time to the remaining client machines upon loading into the game. Since the optimization would be completed prior to playing the game itself, all of the parameters would remain static and would not need to update after first loading the level.
CHAPTER 5. RESULTS

5.1 Games

Using a mathematical formula, coupled with a simulated annealing optimization algorithm, we were able to successfully create a procedural generation system which can create random game levels for two different cooperative virtual reality games. Adjusting the target coop parameter has noticeable and expected impacts upon the content placed in the scene. For example, increasing the target coop value for dungeon levels increases the number of enemies, hazards, and required keys, while decreasing player health and the number of lit torches.

Figure 20: An example of dungeons generated with a target coop value of 1

Figure 21: An example of a dungeon generated with a target coop value of 3.5
5.2 Results

To test the speed and efficacy of the generation algorithm, we ran a series of 10 (n=10) test cases for the dungeon crawl RPG game, generating 10 unique levels for target coop values of 1 and 3.5. The average time taken for these optimizations to reach completion (for 3000 maximum iterations), was around 44 seconds. This also includes the time taken for loading in assets and models (which can increase depending on the complexity of assets and the number of unique assets). When the optimization ran for the full 3000 iterations without reaching its other stopping condition, it would run for around a minute. Occasionally, it would reach its stopping condition from finding a low cost solution early, terminating the algorithm. The quickest solution was 15.4 seconds long and had a cost of 0.0. The longest solution had a duration of 62.08 seconds and had a total cost of 0.14.
From the graph above showing the solution cost over time, the three different discrete temperature intervals can be seen. As the optimization progresses, the chances of accepting bad moves decreases significantly. This is clearly portrayed in the graph of the cost over time in the diminishing frequency of spikes, eventually leading to a flat line at a near-zero cost.

When looking at the individual parameters, it can be clearly seen that those with higher target coop values feature more enemies, more hazards, lower player health, more required keys, and fewer lit torches. Given that the optimization can prefer one parameter over another for reaching its target coop amount, the deviations among these parameters for medium target coop value runs
are high. For example, one optimization solution may have a high enemy count to reach the coop value while another may have very few enemies, relying on other methods.

Figure 25: The average time taken and total solution cost with target coop values of 1 and 3.5

Figure 26: The average enemy count and required keys with target coop values of 1 and 3.5

Figure 27: The average player health and hazard value with target coop values of 1 and 3.5
Figure 28: The average percentage of lit torches with target coop values of 1 and 3.5

For comparison, a test level for the dungeon game was manually created to best show the time which can be saved using procedural generation. In total, this took around 35 minutes to complete. This process required the following steps:

- Placing the room patches while counting the room value
- Placing the correct number of enemies
- Placing the correct number of chests with keys
- Updating the main door to match the number of required keys
- Deleting the extra locks
- Updating the torch lit status
  - Calculating the torch lit percentage
- Locking/blocking doors
- Placing traps
- Placing the player prefabs
- Updating the players’ health
- Setting up the current room variable for each enemy to handle their navigation

5.3 Issues

There are several moves which can create conflict with one another during the optimization process. Two such move pairs are removing rooms and increasing the required keys. In the case of removing a room, the content within the room being deleted can have a significant impact on the other optimized parameters, undoing several iterations of previous work done by the algorithm. A potential solution to this issue would be to run the optimization in different “phases,” each with its own temperature and number of iterations. For instance, the first phase
would only consist of the room layout itself, without placing any content inside. After this, the game would then move on to deciding upon parameters, and then work on the actual placement of objects in the level. This division would solve numerous problems, including the aforementioned issue of having content being removed as well as the issue with earlier-added rooms being more likely to receive content given that they are present in the optimization longer. In the case of increasing the required amount of keys, this parameter frequently conflicts with the number of keys in the scene. Given there must be enough keys in the scene to meet the requirement, solutions that do not meet this criteria are not acceptable. The current solution to this issue is to simultaneously propose moves for increasing the required keys and adding a new key.

Another issue that was noticed with some moves which have very small total impacts on the level. For instance, given the large number of torches in a dungeon level, the original “light torch” and “unlight torch” had very little change and the total torch lit percentage never deviated much from its initial value. To remedy this, a loop was set up to propose the same move multiple times (5 times in this case).

5.4 Parameter Tuning

During the creation of the optimization algorithm, several parameters needed to be tuned to give optimal results. The most important of these variables is the temperature weight. This variable factors into the probability acceptance function along with the temperature. The tested range was from 1-100 with 50 being the final chosen value. Too low of a value can result in the algorithm accepting too many bad moves and not reaching an acceptable cost. Too high values for this parameter could result in only good moves being accepted, defeating the purpose of the annealing algorithm to begin with.

In addition to the cooling rate, the maximum and minimum cooperation values for several parameters were needed. These are used in the inverse linear interpolation function which is part of the coop cost term. An example of this is the number of enemies in the scene. A minimal coop solution will have 1 enemy and a maximum cooperation solution will have 4. In addition to these interpolated values, solutions proposing any value outside of the maximum will be rejected. The
main parameters which needed adjustment to reach optimal solutions were the number of required keys and the number of enemies.

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Minimum Coop Value</th>
<th>Maximum Coop Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>Number Enemies</td>
<td>4</td>
<td>1</td>
</tr>
<tr>
<td>Player Health</td>
<td>200</td>
<td>50</td>
</tr>
<tr>
<td>Required Keys</td>
<td>1</td>
<td>5</td>
</tr>
<tr>
<td>Hazard Value</td>
<td>3</td>
<td>10</td>
</tr>
<tr>
<td>Torch Lit Percent</td>
<td>100</td>
<td>0</td>
</tr>
</tbody>
</table>

5.5 Cooling Rate

As mentioned previously, the simulated annealing algorithm makes use of a temperature parameter which decreases throughout the optimization process. A higher temperature value results in more “bad” or sub-optimal moves being accepted, increasing the variability of the results and helping to overcome local minimums. The temperature is decreased over the course of the optimization. Lower temperature lead to reduced probability of move acceptance, bringing the decision making process closer to that of a greedy algorithm as the temperature falls from 1 to 0. For this project, rather than having the temperature decrease gradually over time, we instead chose to make use of discrete temperature intervals. The optimization runs for a maximum of 3000 iterations and temperature values range from 0.0 to 1.0. The final intervals chosen are as follows: a temperature of 1 for the first 1000 iterations, 0.5 for 1001-2000, and 0.25 for the remainder of the optimization.

This method was chosen over a gradual decline for several reasons. Firstly, it allows us to clearly see the relationship between the acceptance probability of moves as a result of the temperature. Secondly, this method allows us to have different move probabilities for each temperature interval. For instance, the “add rooms” move is given a higher probability at the start of the optimization with a lower probability later due to its more drastic effect on the solution relative to other moves. With this additional system in place, the temperature intervals control not only
the probability of accepting moves, but also the probability of proposing certain types of moves, further allowing for an increase of volatility early on and a phase of refinement as it approaches the end. This method is similar to the method employed by Xie et al. in their study in which they decreased the temperature value “by 0.1 every 3,000 iterations, until it reaches zero” (Xie, et al. 2018), although using fewer total iterations and fewer discrete intervals.
CHAPTER 6. LIMITATIONS AND DESIGN GUIDELINES

6.1 Limitations

Due to health concerns resulting from the Covid-19 outbreak, coupled with the cooperative virtual reality nature of this project, we were not able to perform the proposed user studies. As mentioned in the previous section, there are several potential experiments which can be derived from the work completed as part of this project. There are several factors which make this study particularly difficult to be conducted remotely while following social distancing rules, including: the VR nature of the study, the small population of users with personal VR headsets, and the fact that the study requires two participants simultaneously.

6.2 Design Guidelines

Below are included some suggestions for developers and researchers looking to utilize similar methods of procedural generation.

- Developers looking to similarly work with VR should follow the standard guidelines for VR games (such as those to avoid motion sickness)
- Patch-based methods of generation greatly simplify the generation process
- Using a smaller number of optimized parameters will greatly simplify the optimization process and the total cost term function
- When developing for VR, considerations should be taken with regards to polygon count to maintain an optimal performance at high resolutions
7.1 Conclusions

In this project, we demonstrate the usage of a mathematical cost term function to control the procedural generation for cooperative games. We were able to generate and tune an algorithm using mathematical cost function to create this game content. Results from several case levels show that the optimization can successfully create levels with higher or level of cooperative elements based on a target cooperative element parameter. Additionally, the system was able to create levels consistently and with a low cost (as long as the target coop value is within an acceptable range of ~1-4).

7.2 Future Work

There are potential areas for future development for this project. Firstly, the same algorithm can be tested with more game genres and game formats to show its generalizability. The same methods could even be tested using non-entertainment simulations or educational games to test its validity in more serious cases.

In addition to applying this same generation method/algorithm to more types of games, better methods of evaluation can be designed. For the proposed experiment, the main methods of evaluation would be a custom questionnaire and other minor metrics such as time for completion and the number of vocal interactions between players. However, more robust methods of evaluating the levels and their impact on cooperation can be researched and implemented.

The current optimization algorithm performs all move variants (i.e. level moves, items moves, hazard moves, etc.) throughout the entire optimization. However, a more robust generation system would perhaps opt to perform the generation in certain fixed "stages." For example, the system could first generate all the rooms and the layout of the level before deciding to place anything inside the rooms. This could help ensure a more even density of content throughout the level as well as removing the need for moving content in the case of a game patch.
REFERENCES


Ramos, R. P. Procedural Content Generation for Cooperative Games.


Smith, G. "The future of procedural content generation in games." Tenth Artificial Intelligence and Interactive Digital Entertainment Conference. 2014.


APPENDIX A. QUESTIONNAIRE

1. **Our team had a shared goal or objective**
   - 1
   - 2
   - 3
   - 4
   - 5
   - Strongly Disagree
   - Disagree
   - Neutral
   - Agree
   - Strongly Agree

2. **Our team worked together effectively to complete our goal**
   - 1
   - 2
   - 3
   - 4
   - 5
   - Strongly Disagree
   - Disagree
   - Neutral
   - Agree
   - Strongly Agree

3. **Team problem solving resulted in effective solutions**
   - 1
   - 2
   - 3
   - 4
   - 5
   - Strongly Disagree
   - Disagree
   - Neutral
   - Agree
   - Strongly Agree

4. **My team member contributed adequately towards completing our goal**
   - 1
   - 2
   - 3
   - 4
   - 5
   - Strongly Disagree
   - Disagree
   - Neutral
   - Agree
   - Strongly Agree

5. **I contributed adequately towards completing our goal**
   - 1
   - 2
   - 3
   - 4
   - 5
   - Strongly Disagree
   - Disagree
   - Neutral
   - Agree
   - Strongly Agree

6. **Our individual contributions were equal in completing our goal**
   - 1
   - 2
   - 3
   - 4
   - 5
   - Strongly Disagree
   - Disagree
   - Neutral
   - Agree
   - Strongly Agree

7. **My team member participated for the entire duration of the experience**
   - 1
   - 2
   - 3
   - 4
   - 5
   - Strongly Disagree
   - Disagree
   - Neutral
   - Agree
   - Strongly Agree

8. **I participated for the entire duration**
   - 1
   - 2
   - 3
   - 4
   - 5
   - Strongly Disagree
   - Disagree
   - Neutral
   - Agree
   - Strongly Agree

9. **The game levels which I played felt as if they were designed manually**
   - 1
   - 2
   - 3
   - 4
   - 5
   - Strongly Disagree
   - Disagree
   - Neutral
   - Agree
   - Strongly Agree
APPENDIX B. CODE SNIPPETS

Figure A.1: Code snippet of the total cost function for the dungeon game

```java
// begin computing the game cost
float enemyCovalue = Mathf.InverseExp(dungeonScript.minCovalueRadius, dungeonScript.maxCovalueRadius, dungeonScript.currentCovalueRadius);
float trapCovalue = Mathf.InverseExp(dungeonScript.minTrapCovalue, dungeonScript.maxTrapCovalue, dungeonScript.currentTrapCovalue);
float itemCovalue = Mathf.InverseExp(dungeonScript.minItemCovalue, dungeonScript.maxItemCovalue, dungeonScript.currentItemCovalue); +
float playerCovalue = Mathf.InverseExp(dungeonScript.minPlayerDistance, dungeonScript.maxPlayerDistance, dungeonScript.currentPlayerDistance); +
// have up the cov value from each of the previous elements:
float totalCovalue = trapCovalue + enemyCovalue + playerCovalue + itemCovalue;
//compute the fare based on the cov value distance from ideal value:
float fare = Mathf.Abs(cityScript.idealCovalue - totalCovalue);
// begin computing the layout
layoutCost = Mathf.Abs(dungeonScript.currentRoomValue - dungeonScript.idealRoomValue);
variationCost = Mathf.Abs(dungeonScript.duplicateRoomValue * (dungeonScript.duplicateRoomValue - dungeonScript.idealRoomValue));

// total cost = layoutCost + variationCost;

if (costlevel = (layoutweight + layoutCost) + (variationweight + variationCost);

float total = fare + costlevel;
return total;
```

Figure A.2: Code snippet of the move acceptance function

```java
public static bool ProposeTotalCostMoveCheck(string parameter)
{
float c = controller.CalculateTotalCurrentCosts(); // gets current cost
float p = controller.CalculateTotalProposedCosts(); // gets the cost of a proposed move
if (Mathf.Abs(c) > Mathf.Abs(p)) // accept good move if proposed cost is less than the current cost
{
controller.plotter.addLine(controller.costtotal, c, p, parameter, "accept");
return true;
}
else // bad move
{
float costOfCurrent = Mathf.Abs(c);
float costOfProposed = Mathf.Abs(p);
float delta = Mathf.Abs(costOfProposed - costOfCurrent);
float chance = Mathf.Exp(-delta / (controller.currentTemperature / controller.temperatureWeight)); // chance to accept bad move
if (Random.Range(0f, 1f) < chance) // accept bad move due to probability
{
return true;
}
return false; // reject bad move
}
return false;
}
```
Figure A.3: Code snippet of the city game’s level move, along with the swap building function