

Source code (c++) of the simulation

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// This code is written by Md. Rajib Arefin
// Date: 20/05/2019
// This c++ code is written to simulate a mean-field approach in vaccination game to explore...
// ...individuals vaccination dilemma in influenza vaccine uptake depending upon cost and efficacy
// This source code can serve as the base program for generating data for Figs. 4 - 7 and 9
// Specifically, this code generates data for all C_Q vs C_T heatmaps in Fig. 4. with fixed e_Q,
e_T_B
// By changing parameter settings, all other heatmaps can be generated

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#include <iostream>
#include <fstream>
#include <stdio.h>
#include <math.h>
#include <vector>
#include <list>
#include <string.h>
#include <stdlib.h>
#include <ctype.h>
#include <sstream>
#include <string>
#include <cstdio>
#include <time.h>
#include <iomanip>
using namespace std;
using std::setw;

int main()
{
# define times 300
# define GENERATION 1000
# define cost 100
# define quality 100
# define K 0.1 // sensitivity constant used in Fermi rule
// defining transmission rate and recovery rate parameters
# define B1 0.5 //
# define B2 0.5
# define G1 0.2
# define G2 0.2
// creating csv file for storing several results coming from the simulation
string file1 = "total_infected_fraction.csv";
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ofstream Data1(file1);
Data1 << "C_Q,C_T,R" << endl;

string file2 = "VC_Q.csv"; // vaccination coverage (QIV)
ofstream Data2(file2);
Data2 << "C_Q,C_T,V_Q" << endl;

string file3 = "VC_T.csv"; // vaccination coverage (TIV)
ofstream Data3(file3);
Data3 << "C_Q,C_T,V_T" << endl;

string file4 = "ASP.csv"; // average social payoff
ofstream Data4(file4);
Data4 << "C_Q,C_T,asp" << endl;

string file5 = "total vaccination coverage.csv";
ofstream Data5(file5);
Data5<< "C_Q,C_T,vaccination_coverage" << endl;

string file6 = "fes_A.csv"; // infection by flu A virus
ofstream Data6(file6);
Data6 << "C_Q,C_T,fesA" << endl;

string file7 = "fes_B.csv"; // infection by flu B virus
ofstream Data7(file7);
Data7 << "C_Q,C_T,fesB" << endl;

// Declaring several variables for epidemic dynamics
double S[times + 1], VQ[times + 1], VT[times + 1], IA[times + 1], IB[times + 1],
       R[times + 1];

// several variables for flux calculations
double S1[times + 1], S2[times + 1],V1[times + 1],V2[times + 1],FA[times + 1],FB[times + 1];
double IfaVQ[times + 1], IfbVQ[times + 1], IfaVT[times + 1], IfbVT[times + 1];//several flux
double x[GENERATION + 1]; // fraction of QIV vaccinees
double y[GENERATION + 1]; // fraction of TIV vaccinees
double asp[GENERATION + 1]; // average social payoff
double C_Q, C_T, e_Q, e_T_A, e_T_B;// cost and effectiveness parameters
double HVQ, IVQ, SFR, FFRa, HVT, IVT, FFRb; // outcome of the epidemic (several fractions)
// several transitional probabilities
double phVQ_NV, phVQ_VT, piaVQ_NV, pibVQ_NV, pibVQ_VT, phVT_NV, piaVT_NV, pibVT_NV, piaVT_VQ,
pibVT_VQ, piaVQ_VT;

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double psfr_VQ, psfr_VT, pffra_VQ, pffra_VT, pffrb_VQ, pffrb_VT, VC_Q, VC_T, piVQ_VT,
phVT_VQ, NV;
double pi_Q, pi_T, pi_NV; // average payoff for QIV, TIV, and non-vaccinees

x[0] = 1.0 / 3.0; y[0] = 1.0 / 3.0; // initial value of QIV and TIV vaccinees
e_Q = 0.6; e_T_B = 0.4;
for (int cs = 0; cs < cost + 1; cs++) // Calculating cost for QIV vaccine (loop 1)
{
    C_Q = cs / 100.0;
    for (int cc = 0; cc < C_Q * 100 + 1; cc++) //Calculating cost for TIV vaccine
(C_T<=C_Q) (loop 2)
    {
        C_T = cc / 100.0;
        for (int j = 0; j < GENERATION; j++)// number of seasons/episode loop (loop 3)
        {
            IA[0] = 0.00001;IB[0] = 0.00002; R[0] = 0.0;// initializing infected
fractions and recovered fractions
            VQ[0] = x[j]; VT[0] = y[j]; IfbVT[0] = 0.0; IfaVT[0] = 0.0; IfbVQ[0] =
0.0; IfaVQ[0] = 0.0;

            S[0] = 1.0 - x[j] - y[j] - IA[0] - IB[0]; FA[0] = 0.0; FB[0] = 0.0;
            S1[0] = 0.0; S2[0] = 0.0; V1[0] = 0.0; V2[0] = 0.0;
            e_T_A = e_Q;
            for (int i = 0; i < times; i++){//SIR dynamics with vaccinations (loop 4)
                S[i + 1] = S[i] - S[i] * (B1 * IA[i] + B2 * IB[i]);

                VQ[i + 1] = VQ[i] - (VQ[i] - e_Q * VQ[0]) * B1 * IA[i] - (VQ[i] - e_Q *
VQ[0]) * B2 * IB[i];

                VT[i + 1] = VT[i] - (VT[i] - e_T_A * VT[0]) * B1 * IA[i] - (VT[i] -
e_T_B * VT[0])* B2 * IB[i];

                IA[i + 1] = IA[i] + B1 * IA[i] * (S[i] + VQ[i] - e_Q * VQ[0]) + (VT[i] -
e_T_A * VT[0])* B1 * IA[i] - G1 * IA[i];

                IB[i + 1] = IB[i] + B2 * IB[i] * (S[i] + VT[i] - e_T_B * VT[0]) + (VQ[i]
- e_Q * VQ[0]) * B2 * IB[i] - G2 * IB[i];

                R[i + 1] = R[i] + G1 * IA[i] + G2 * IB[i];

                // calculating several fluxes
                S1[i + 1] = S1[i] + S[i] * B1 * IA[i]; // calculating flux for failure
free rider for A virus

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S2[i + 1] = S2[i] + S[i] * B2 * IB[i]; // calculating flux for failure
free rider for B virus

// calculating flux for infected but vaccinated people (QIV)
V1[i + 1] = V1[i] + (VQ[i] - e_Q * VQ[0]) * B1 * IA[i] + (VQ[i] - e_Q *
VQ[0]) * B2 * IB[i];

// calculating flux for infected but vaccinated people (TIV)
V2[i + 1] = V2[i] + (VT[i] - e_T_B * VT[0]) * B2 * IB[i] + (VT[i] -
e_T_A * VT[0]) * B1 * IA[i];

//total infection with flu A
FA[i + 1] = FA[i] + B1 * IA[i] * (S[i] + VQ[i] - e_Q * VQ[0]) + (VT[i] -
e_T_A * VT[0]) * B1 * IA[i];

//total infection with flu B
FB[i + 1] = FB[i] + B2 * IB[i] * (S[i] + VT[i] - e_T_B * VT[0]) + B2 *
(VQ[i] - e_Q * VQ[0]) * IB[i];

// flux from VQ to A virus
IfaVQ[i + 1] = IfaVQ[i] + (VQ[i] - e_Q * VQ[0]) * B1 * IA[i];
// flux from VQ to B virus
IfbVQ[i + 1] = IfbVQ[i] + (VQ[i] - e_Q * VQ[0]) * B2 * IB[i];
// flux from VT to A virus
IfaVT[i + 1] = IfaVT[i] + (VT[i] - e_T_A * VT[0]) * B1 * IA[i];
// flux from VT to B virus
IfbVT[i + 1] = IfbVT[i] + (VT[i] - e_T_B * VT[0]) * B2 * IB[i];
} // loop 4 ends here

// outcome of the epidemics
HVQ = VQ[times]; HVT = VT[times]; // healthy QIV and TIV vaccinees
// QIV and TIV vaccinees but infected
IVQ = IfaVQ[times] + IfbVQ[times]; IVT = IfaVT[times] + IfbVT[times];
FFRa = S1[times]; FFRb = S2[times]; // failed free riders
SFR = S[times]; // successful free riders
pi_Q = (HVQ * (-C_Q) + IVQ * (-C_Q - 1.0)) / (HVQ + IVQ); // average
payoff for QIV vaccinees
pi_T = (HVT * (-C_T) + IVT * (-C_T - 1.0)) / (HVT + IVT); // average
payoff for TIV vaccinees
pi_NV = (SFR * (0.0) + (FFRa + FFRb) * (-1.0)) / (SFR + FFRa + FFRb); //
average payoff for non-vaccinees
asp[j] = -C_Q * HVQ - C_T * HVT - (C_Q + 1) * IVQ - (C_T + 1) * IVT - (FFRa
+ FFRb);

// transition probabilities (Fermi rule)
phVQ_NV = 1.0 / (1 + exp(-(pi_NV - (-C_Q)) / K)); // P(healthy
vaccinators(QIV) copying non-vaccinators' strategy)

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phVQ_VT = 1.0 / (1 + exp(-(pi_T - (-C_Q)) / K));
piaVQ_NV = 1.0 / (1 + exp(-(pi_NV - (-C_Q - 1)) / K));
pibVQ_NV = 1.0 / (1 + exp(-(pi_NV - (-C_Q - 1)) / K));
piaVQ_VT = 1.0 / (1 + exp(-(pi_T - (-C_Q - 1)) / K));
pibVQ_VT = 1.0 / (1 + exp(-(pi_T - (-C_Q - 1)) / K));
phVT_NV = 1.0 / (1 + exp(-(pi_NV - (-C_T)) / K));
phVT_VQ = 1.0 / (1 + exp(-(pi_Q - (-C_T)) / K));
piaVT_NV = 1.0 / (1 + exp(-(pi_NV - (-C_T - 1)) / K));
pibVT_NV = 1.0 / (1 + exp(-(pi_NV - (-C_T - 1)) / K));
piaVT_VQ = 1.0 / (1 + exp(-(pi_Q - (-C_T - 1)) / K));
pibVT_VQ = 1.0 / (1 + exp(-(pi_Q - (-C_T - 1)) / K));
psfr_VQ = 1.0 / (1 + exp(-(pi_Q - 0) / K));
psfr_VT = 1.0 / (1 + exp(-(pi_T - 0) / K));
pffra_VQ = 1.0 / (1 + exp(-(pi_Q - (-1.0)) / K));
pffra_VT = 1.0 / (1 + exp(-(pi_T - (-1.0)) / K));
pffrb_VQ = 1.0 / (1 + exp(-(pi_Q - (-1.0)) / K));
pffrb_VT = 1.0 / (1 + exp(-(pi_T - (-1.0)) / K));

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// total fraction of QIV, TIV and non-vaccinees
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VC_Q = HVQ + IVQ; VC_T = HVT + IVT; NV = SFR + FFRa + FFRb;
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// evolutionary dynamics of QIV vaccinees
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x[j + 1] = x[j] - HVQ * NV*phVQ_NV - IfaVQ[times] * NV*piaVQ_NV -
IfbVQ[times] * NV*pibVQ_NV - HVQ * VC_T*phVQ_VT - IfaVQ[times] * VC_T*piaVQ_VT - IfbVQ[times] *
VC_T*pibVQ_VT + SFR * VC_Q*psfr_VQ + FFRa * VC_Q*pffra_VQ + FFRb * VC_Q*pffrb_VQ + HVT * VC_Q*phVT_VQ
+ IfaVT[times] * VC_Q*piaVT_VQ + IfbVT[times] * VC_Q*pibVT_VQ;

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// evolutionary dynamics of TIV vaccinees
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y[j + 1] = y[j] - HVT * NV*phVT_NV - IfaVT[times] * NV*piaVT_NV -
IfbVT[times] * NV*pibVT_NV - HVT * VC_Q*phVT_VQ - IfaVT[times] * VC_Q*piaVT_VQ - IfbVT[times] *
VC_Q*pibVT_VQ + SFR * VC_T*psfr_VT + FFRa * VC_T*pffra_VT + FFRb * VC_T*pffrb_VT + HVQ *
VC_T*phVQ_VT + IfaVQ[times] * VC_T*piaVQ_VT + IfbVQ[times] * VC_T*pibVQ_VT;

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} // loop 3 ends here
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// saving data in csv file
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Data1 << C_Q << "," << C_T << "," << R[times] << endl;
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Data2 << C_Q << "," << C_T << "," << x[GENERATION] << endl;
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Data3 << C_Q << "," << C_T << "," << y[GENERATION] << endl;
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Data4 << C_Q << "," << C_T << "," << asp[GENERATION - 1] << endl;
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Data5 << C_Q << "," << C_T << "," << x[GENERATION] + y[GENERATION] << endl;
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Data6 << C_Q << "," << C_T << "," << FA[times] << endl;
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Data7 << C_Q << "," << C_T << "," << FB[times] << endl;
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} // loop 2 ends here
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} // loop 1 ends here  
Data1.close();  
Data2.close();  
Data3.close();  
Data4.close();  
Data6.close();  
Data7.close();  
} // program ends here
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