Abstract— Massive multiple-input multiple-output (MIMO) systems operating in the centimeter-wave (cmWave) and millimeter-wave (mmWave) region offer huge spectral efficiencies, which enable to satisfy the urgent need for higher data rates in mobile communication networks. However, the proper design of those massive MIMO systems first requires a deep understanding of the underlying wireless propagation channel. Therefore, we present a fully-digital MIMO measurement system operating around 28 GHz. The system enables to take fast subsequent snapshots of the complex MIMO channel matrix. Based on this method we statistically analyze the time-dependent channel behavior, the achievable signal quality and spectral efficiency, as well as the channel eigenvalue profile. Furthermore, the presented calibration approach for the receiver enables an estimation of the dominant absolute angle of arrival (AoA) and allows us to draw conclusions about the line-of-sight (LOS) dominance of the scenario. In total, 159 uplink communication measurements over 20 seconds are conducted in three different small cell site scenarios to investigate the wireless propagation behavior. The measurements reveal the existence of several spatial propagation paths between the mobile transmitter and the base station. Furthermore, an insight into their likelihood in different propagation scenarios is also given.

Index Terms—Channel estimation, MIMO communication, Mobile communication

I. INTRODUCTION

More than ever before, mobile wireless communication networks demand for higher data rates. To meet these requirements research and industry focus in particular on exploiting the large available spectral resources in the cmWave and mmWave region, the decrease of the the cell size to increase the spectral reuse, and the utilization of MIMO systems to achieve a spatial multiplexing gain [1]–[5]. As a result, the 3rd generation partnership project (3GPP) lately defined the n257-band between 26.5 GHz - 29.5 GHz offering 3 GHz of spectral bandwidth [12].

To investigate the achievable data rates of massive MIMO communication systems in the n257-band and answer important system design questions, a deep understanding of the wireless propagation channel is required. Note that the propagation conditions determine the expected channel capacity of MIMO systems [13]. In practice, MIMO algorithms and architectures are evaluated in numerical simulations on the basis of models of the wireless propagation channel [14]. Nevertheless, these channel models depend on simplifications of the complicated electromagnetic propagation and thereby never fully reproduce the propagation effects [15]. For these reasons, extensive measurement campaigns have to be performed to characterize the wireless propagation channel and demonstrators are needed to verify the performance and validate channel models.

A. Channel Measurements around 28 GHz

Till date, many research groups realized channel sounding systems to investigate the propagation characteristics around 28 GHz as presented in [16]–[46]. Particularly worthy to mention are the extensive measurement campaigns by Rappaport et al. for the 28, 38, 60, and 73 GHz mmWave bands summarized in [16]. At 28 GHz the results for urban scenarios reveal path loss exponents of 2.1 for line-of-sight (LOS) and 3.4 for non-line-of-sight (NLOS) scenarios, which are similar to today’s microwave path loss models [16], [47], [48].

Another important research aspect in wireless channel sounding is the analysis of the dynamic channel behavior. Therefore, the required measurement times to acquire the channel characteristics at each transmitter and receiver location have to be reduced. To better temporally analyze the wireless propagation channel Bas & Molisch et al. present in [17], [49] a MIMO channel sounder at 28 GHz based on a phased array structure that performs fast beam steering. Compared to channel sounders with rotating horn antennas

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the measurement time could drastically be reduced down to milliseconds [17]. The channel sounder is used to analyze the outdoor to indoor propagation channel in [50], [51] and to estimate the angular spectrum, delay spread, and Doppler spectrum in an outdoor micro cellular scenario in [52]. A different approach reducing the channel measurement time is introduced by Tataria & Tufvesson et al. in [19]. The presented MIMO channel sounder measures the $256 \times 128$ dual-polarized channel by switching between the different elements. In contrast to previous works, snapshots of the MIMO channel can be acquired in 380 ms.

Beside the extensive channel characterization efforts made, first MIMO demonstrators operating within the $n257$-band have been presented in literature. Researchers from Samsung Electronics demonstrated in [53] first indoor and outdoor coverage tests using a subarray-based (sub-connected) hybrid beamforming testbed. This work was extended in [54] achieving data rates of up to 7.5 Gbps by transmitting four parallel data streams to two mobile stations in close distance. Recently, Yang et al. reported in [55] the first fully digital massive MIMO transceiver operating at 28 GHz consisting of 64 antenna elements. In the demonstrator test 20 non-coherent data streams could be transmitted at the same time to eight user entities resulting in a spectral efficiency of 101.5 bps/Hz.

Further MIMO communication measurements are presented by NTT Doicom in [56]–[58].

**B. Main Contributions**

To tackle the problem of long measurement times of current channel sounders and analyse achievable communication data rates within realistic small cell scenarios, we present a fully digital $16 \times 4$ MIMO measurement system operating around 28 GHz. Unlike the channel sounders presented above, we analyze the wireless propagation behavior by estimating and evaluating subsequent snapshots of the complex MIMO channel matrix, representing the time-dependent channel response between each transmit and receive antenna assuming a frequency non-selective channel [59]. This method enables us to take snapshots of the channel in much less than a millisecond allowing a good analysis of the dynamic propagation behavior. The main contributions can be summarized as follows:

- This work presents a method to rapidly acquire narrowband snapshots of the complex MIMO channel matrix, which enables us to investigate the wireless propagation behavior around 28 GHz.
- We verify this approach and analyze the MIMO wireless propagation channel in a total of 159 measurements in three different small cell site scenarios. For each measurement the mobile unit is placed at a different location and the received data is recorded for around 20 s. Snapshots of the MIMO channel are estimated for each symbol, i.e. each 128 μs.
- A calibration approach for fully digital MIMO architectures is presented and implemented at the receiver allowing the correction of amplitude and phase imbalances between the receive branches. This facilitates the estimation of the dominant absolute AoA. With simultaneous determination of the spatial positions of transmitter and receiver as well as the receiver orientation, the found AoA allows to draw conclusions about the LOS dominance of the scenario.
- We present for the first time measurement results for the channel eigenvalue statistics around 28 GHz. This statistic reveals with which likelihood up to four spatial propagation paths can be utilized. Note that the eigenvalues of the channel determine if spatial multiplexing (Blast-type) communication techniques are wise to be applied [11].
- Furthermore, the subsequent snapshots of the MIMO channel matrix are used to evaluate the achievable spectral efficiencies. The measurement results give information about the degradation in spectral efficiency caused by foliage within the wireless propagation paths, as the coherence time is reduced.

It should be noted, that our MIMO communication demonstrator does not aim to replace current channel sounder, but rather serves as an complementary approach to analyze the so far insufficiently investigated channel characteristics, as for example the time-dependent eigenvalue profile of the channel. In advance the measured snapshots of the channel matrix can be directly fed into measurement-based MIMO channel models, to numerically analyze novel MIMO communication architectures and algorithms. Note that new architectures and algorithms are mostly evaluated in numerical simulations utilizing abstract MIMO channel models as presented in [60]–[64].

This work is organized as follows. Section II presents the hardware setup as well as the methods for receiver calibration and channel estimation. In section III the outdoor measurement scenarios are described in detail. Finally, section IV discusses the results of the channel analysis around 28 GHz.

**II. MIMO CHANNEL MEASUREMENT APPROACH**

To investigate the behavior of the wireless propagation channel around 28 GHz we developed a fully-digital MIMO measurement system. The system is designed to measure the multipath channel characteristic emulating an uplink communication scenario between a mobile user with $M_{\text{ant}} = 4$ transmitters and a base station with $N_{\text{ant}} = 16$ receivers. In this section we introduce the designed hardware setup and explain the developed channel estimation and system calibration approach. Furthermore, the estimation of the dominant AoA is explained and the modulation error ratio (MER) is discussed as a metric for assessing signal quality.

**A. System Setup**

The measurement system consists of a fully digital $16 \times 4$ MIMO configuration with 4 transmit antennas at the mobile user entity and 16 receive antennas at the base station. The block diagram of the system configuration is shown in Fig. 1. To achieve a high sensitivity, a heterodyne architecture is selected, which enables a flexible adjustment of the radio frequency (RF) and intermediate frequency (IF).
1) Mobile Transmitter: At the transmitter side the training signals for channel estimation are generated by a host computer (PC) connected via Gigabit-Ethernet to two commercial software defined radios (SDRs) of type USRP X310 by Ettus Research. The SDRs include digital-to-analog-conversion (DAC), baseband to IF conversion, as well as IF filtering and amplification.

To translate the IF to the desired RF frequency band, a RF frontend with four symmetrical transmit branches is designed. It consists of a four metal layer printed circuit board (PCB) with a substrate of type RO4003C from Rogers Corporation with a height of 203 μm and a dielectric constant $\varepsilon_r = 3.55$. The IF-to-RF conversion and RF amplification is realized by commercially available monolithic microwave integrated circuits (MMICs). The PCB is integrated into a metallic housing for electromagnetic shielding, protection and better heat dissipation. The mixer includes an internal frequency doubler and the upper sideband of the mixing process is used, resulting in a RF center frequency

$$f_{RF} = 2f_{LO} + f_{IF},$$

where $f_{IF}$ is the IF in the range of 400 MHz to 3.5 GHz and $f_{LO}$ is the externally supplied LO frequency in the range 12 GHz to 13.5 GHz depending on the selected IF. The RF can be set in the range of the n257-band between 26.5 GHz - 29.5 GHz. For all inputs and outputs of the RF frontend module 2.92 mm connectors are utilized. The RF frontend is connected to the SDRs and the antenna via coaxial cables. The measured output 1 dB-compression point of the RF frontend is 10 dBm.

For the mobile transmitter four monopole antennas are mounted on a metallic housing to enable a 360° coverage in the azimuth plane. This makes the mobile transmitter independent of a rotation in azimuth. The monopole antennas have a height of $\lambda_0/4$ at 28 GHz to avoid dips in the elevation radiation pattern. In elevation the measured half power beamwidth (HPBW) is 26° with a main beam direction of 20.5° upwards originating from the ground plane of the monopoles. The tilt by 20.5° upwards is selected to be a good fit for the considered application scenario, where the base station is installed on an elevated position. The measured maximum realized element gain including connector and feed line losses is 1.5 dBi. The monopoles are arranged in a square separated by 0.55 $\lambda_0$ at 28 GHz to achieve uniform coverage in azimuth over the entire 360° range. If the antennas are not properly spaced, notches in the azimuth radiation pattern would occur.

For the later measurement campaign the RF frontend and SDRs are integrated within a transportable box and placed together with the DC power supply and LO signal generator on a trolley shown in Fig. 2(c).

2) Base station: At the base station or receiver side a 16 antenna element board is designed with an element spacing of 5.35 mm, which relates to a spacing of $\lambda_0/2$ at 28 GHz. All antenna elements are realized as microstrip patch antennas using the same four metal layer RO400C PCB as for the RF frontend. To increase the antenna element gain two serially fed microstrip patch elements are vertically stacked, narrowing down the HPBW in elevation direction to 40.8°. The HPBW in azimuth is 86°. The measured realized element gain, including the connector and feed line losses, is 4.1 dBi. A photo of the front of the antenna board is shown in Fig. 2(a).

The 16 RF outputs of the antenna board are connected via coaxial cables to four RF backends each consisting of four symmetric channels performing low noise amplification, bandpass filtering and RF-to-IF conversion. The RF backends are constructed according to the same scheme as for the RF frontends utilizing a four metal layer RO400C PCB, commercial available MMICs, 2.92 mm connectors and a
metal housing adapted to the PCB. Furthermore, the antenna board is mounted together with the RF backend modules onto a metallic construction, which allows a manual adjustment of the antenna elevation angle. The LO signal for RF-to-IF down-conversion is, similar to the transmitter side, supplied externally at half the mixing frequency to each RF frontend as shown in Fig. 1.

Finally, the received and digitized data is transferred via Ethernet to a host PC, where online and offline post-processing is performed. The receiver noise figure (NF) is calculated based on the information given in the data sheets of the used components to NF \( \approx 2.1 \) dBi.

3) **Transmitter and receiver clock and frequency synchronization**: GPS-disciplined, oven controlled crystal oscillators (GPSDOs) by Ettus Research are employed to synchronize the SDRs and LO signal generators at the transmitter and receiver side. The GPSDOs provide a high-accuracy 10 MHz reference with phase noise of \(-110\) dBC/Hz at 10 Hz and a pulse-per-second (PPS) signal to ensure a synchronous sampling between the SDRs. At the transmitter the GPSDO is integrated into the first SDR. The 10 MHz reference and PPS are forwarded from the first SDR via daisy-chaining to the second SDR. Moreover the 10 MHz reference is provided to the LO signal generator as shown in Fig. 1. At the receiver the GPSDO is integrated into a OctoClock-G CDA-2990 by Ettus Research. The OctoClock-G CDA-2990 has eight 10 MHz reference and PPS outputs, which are connected to the SDRs at the receiver. The additional SDR for calibration receives the 10 MHz reference and PPS via daisy-chaining. Furthermore, the 10 MHz reference is forwarded by the first SDR via daisy-chaining to the LO signal generator at the receiver. The GPS coordinates provided in this process are also used in the later presented measurement campaigns to determine the spatial position of the transmitter and receiver.

**B. Channel Estimation Principle and Signal Processing**

To estimate the MIMO propagation channel, known training symbols are transmitted at the mobile user entity as it is standard in many communication systems [65], [66]. As signal waveform orthogonal frequency division multiplexing (OFDM) is used. The randomly selected training symbols are modulated using quadrature-phase shift keying (QPSK). OFDM facilitates the separation of the different transmit antennas by using exclusive OFDM subcarriers and enables the estimation of the complex MIMO channel matrix with several measurement points in the frequency domain [67]. By separating the transmit antennas in frequency domain, the transmitters can be separated at each receive antenna, realizing an estimation of the instantaneous complex MIMO channel matrix. The MIMO channel matrix represents the channel response between each transmit and receive antenna assuming a frequency non-selective channel [59]. To fulfill this assumption the signal bandwidth has to be smaller than the coherence bandwidth [68]. This also motivates to utilize OFDM, as the frequency-nonselectivity assumption just needs to be true for the bandwidth of a small range of OFDM subcarriers.

Let \( \mathcal{I} \subseteq \{0, 1, \ldots, N_c - 1\} \) be an index set addressing the \( N_c \) OFDM subcarriers and divide it into a subset of indices \( \mathcal{I}_d \), containing the complex modulated data symbols used for channel estimation purposes and a subset of indices \( \mathcal{I}_0 \), containing the positions of all null carriers. It holds

\[
\mathcal{I}_d \cup \mathcal{I}_0 = \mathcal{I}.
\]

Furthermore, the subset \( \mathcal{I}_0 \) contains the indices of the subcarriers around zero frequency to avoid blockage due to high DC parts \( \mathcal{I}_\text{DC} \subseteq \mathcal{I}_0 \), the indices of upper and lower guard carriers \( \mathcal{I}_\text{guard} \subseteq \mathcal{I}_0 \), and further recessed OFDM subcarriers for receiver calibration \( \mathcal{I}_\text{cal} \subseteq \mathcal{I}_0 \). Hence, no subcarrier index is part of two subsets meaning the sets are disjoint so that

\[
\mathcal{I}_0 = \mathcal{I}_\text{DC} \cup \mathcal{I}_\text{guard} \cup \mathcal{I}_\text{cal}
\]

and

\[
\mathcal{I}_\text{DC} \cap \mathcal{I}_\text{guard} \cap \mathcal{I}_\text{cal} = \emptyset
\]

is fulfilled. The transmit antennas are separated for the channel estimation process using exclusive OFDM subcarriers. Therefore, the index set \( \mathcal{I}_d \) is divided into \( \mathcal{M}_\text{ant} \) subsets \( \mathcal{I}_{d,m} \subseteq \mathcal{I}_d \) with \( m \in \{1, 2, \ldots, \mathcal{M}_\text{ant}\} \) containing the \( \mathcal{I}_{d,m} \) exclusive subcarriers of the \( m \)-th transmit antenna. It holds

\[
\mathcal{I}_d = \bigcup_{m=1}^{\mathcal{M}_\text{ant}} \mathcal{I}_{d,m}.
\]

The OFDM subcarrier indices follow an interleaved assignment to the different transmit antennas to minimize the spacing between two neighboring subcarriers of one subset \( \mathcal{I}_{d,m} \). The OFDM subcarrier spacing is defined as

\[
\Delta f = B_s/N_c = 1/T_o,
\]

where \( B_s \) represents the available signal bandwidth and \( T_o \) the OFDM symbol duration.

Based on the defined index sets the complex OFDM data frame for one OFDM symbol in the frequency domain \( \mathbf{X} \in \mathbb{C}^{\mathcal{M}_\text{ant} \times N_c} \) is constructed. The discrete OFDM time domain signal with sampling time \( t = q \cdot T_o/N_c \) and \( q \in \{0, 1, \ldots, N_c - 1\} \) can be written as [59], [69]

\[
\mathbf{u}(m,q) = \sum_{p=0}^{N_c-1} \mathbf{X}(m,p) \cdot e^{j2\pi pq/N_c},
\]

where \( p \in \{0, 1, \ldots, N_c - 1\} \) denotes the indices for the OFDM subcarrier frequencies \( f_p = p \cdot \Delta f = p/T_o \). The channel response of a multipath channel can be represented by [70], [71]

\[
\mathbf{h}(n,m,q) = \sum_{d=0}^{N_p-1} \mathbf{h}_c(n,m,d,q) \cdot \delta(q-d)
\]

consisting of \( N_p \) replicas of the transmit signal arriving with the discrete delay time in samples \( d \) and complex weighting factor \( \mathbf{h}_c(n,m,d,q) \) at the time sample point \( q \) at the receiver. For the received signal follows with the index set \( n \in \{0, 1, \ldots, \mathcal{M}_\text{ant} - 1\} \) of the receive antennas

\[
\mathbf{y}(n,q) = \sum_{m=0}^{\mathcal{M}_\text{ant}-1} \sum_{d=0}^{N_p-1} \mathbf{h}_c(n,m,d,q) \cdot \mathbf{u}(m,q-d) + \mathbf{n}(n,q),
\]
where $n \in \mathbb{C}^{N_{\text{ant}} \times N_c}$ accounts for the additive white Gaussian noise introduced during transmission. The multiplication of the transmit signals with a time-variant channel would lead to a cyclic convolution in frequency domain and thereby to inter-carrier-interferences (ICI). To avoid ICI the OFDM symbol duration has to be chosen smaller than the coherence time of the channel, so that the complex channel coefficients $h_c(n, m, d, q)$ can be assumed constant over one OFDM symbol. With this assumption the received signal in the frequency or symbol domain results after discrete Fourier transformation (DFT) to

$$R(n, p) = \sum_{m=0}^{M_{\text{ant}}-1} \sum_{d=0}^{N_p-1} \text{DFT}\{H(n, m, d) \cdot u(m, q-d)\} + N(n, p).$$

To avoid inter-symbol-interferences (ISI), the same OFDM symbol is transmitted continuously, thereby omitting the need for a guard interval. Due to the cyclic properties of the transmit sequence the time shifting property of the DFT

$$u(\cdot, q-d) \circlearrowleft X(\cdot, p) \cdot e^{-j2\pi qd/N_c}$$

can be exploited, leading to

$$R(n, p) = \sum_{m=0}^{M_{\text{ant}}-1} \sum_{d=0}^{N_p-1} \text{DFT}\{H(n, m, d) \cdot u(m, q-d)\} e^{-j2\pi pd/N_c} + N(n, p),$$

averaging over all subcarrier of each transmitter assuming a frequency non-selective channel for the full signal bandwidth $B_s = N_c \cdot \Delta f$. It is therefore necessary that the receiver knows the training symbols as well as the OFDM subcarrier indices $I_{d,m}$ of the individual transmitters $\forall m$.

C. System Calibration and AoA Estimation

An important achievement of the hardware design is the determination of the strongest absolute AoA at the receiver. This requires a correction of the imbalances in amplitude and phase between the 16 RF receive branches, which result from cable length deviations, manufacturing tolerances of the PCBs and MMICs, deviations in soldering, and phase differences of the LO signals. Especially the used SDRs cause a random phase offset between the branches because there is no possibility to harmonize the phase of the LO signals for IF up- and down-conversion. Therefore, a calibration branch was added to the hardware design to correct these imbalances. The calibration branch consists of an additional SDR at the receiver generating the calibration signal, which is fed at the IF to a dedicated input port of the receiver antenna board. The receiver antenna board incorporates a mixer which upconverts the calibration signal to RF by means of an externally
supplied LO signal at half the mixing frequency as shown in Fig. 1. The calibration signal is then split symmetrically by a distribution network and added to the receive signal directly behind the 16 antenna elements using a coupled line directional coupler. As the calibration signal is known at the receiver and is symmetrically coupled into each receive path, the relative differences between the amplification and phase of the receive branches can be estimated and corrected in the digital domain of the receiver. The amplitude and phase imbalances have to be only corrected with respect to a selected receiver branch. It is important to mention that to enable a real-time calibration the received and calibration signals have to be separated to avoid interference. This separation is achieved by keeping selected OFDM carriers of the transmitted signal free for the calibration signal. As defined before the OFDM subcarrier calibration index set is denoted by $\mathcal{I}_{\text{cal}}$ and it holds $\mathcal{I}_{\text{cal}} \cap \mathcal{I}_{\text{t}} = \emptyset$. The introduced imbalances are measured for each OFDM symbol in the same manner as in (14) resulting to

$$\hat{d}_n = \frac{1}{|\mathcal{I}_{\text{cal}}|} \sum_{p \in \mathcal{I}_{\text{cal}}} \hat{R}(n, p) \cdot C(n)^{-1},$$

where $\hat{R}$ represents the received baseband signal matrix including the superimposed calibration signal. Finally, the result is used to obtain the calibrated MIMO channel matrix

$$\hat{H}_{\text{cal}} = \hat{D}^{-1} \cdot \hat{H}$$

with the calibration matrix $\hat{D} = \text{diag}\{\hat{d}_0, \ldots, \hat{d}_{N_{\text{ant}}-1}\}$.

Based on the calibrated channel matrix, the strongest AoA $\hat{\phi}_{\text{max}}$ can be determined. Therefore the singular value decomposition (SVD) of the calibrated channel matrix is calculated $\hat{H}_{\text{cal}} = \hat{U} \hat{\Sigma} \hat{V}^H$ to extract the first receiver side beamforming vector $\hat{u}_1 \in \mathbb{C}^{N_{\text{ant}} \times 1}$ of $\hat{U} = [\hat{u}_{1}^H, \ldots, \hat{u}_{N_{\text{ant}}}^H]^T$. The radiation pattern over the azimuth angle $\phi$ using the first receiver side beamforming vector results to

$$C(\phi) = \sum_{n=0}^{N_{\text{ant}}-1} \hat{u}_1^H(n) C_e(n, \phi) e^{jkd(n)\sin\phi},$$

where $\hat{u}_1^H$ denotes the Hermitian transpose of $\hat{u}_1$, $C_e$ contains the antenna element characteristics, $k = 2\pi/\lambda$ denotes the wave number, and $\hat{d}$ represents a vector with the spatial positions of the active antenna elements. As the first receiver side beamforming vector enables a beam steering into the direction of the strongest AoA the corresponding angle can be extracted by finding the maximum in the radiation pattern. The strongest AoA is therefore given by

$$\hat{\phi}_{\text{max}} = \arg\max_{\phi} \{|C(\phi)|\},$$

which can be compared with the physical azimuth angle between the position of the base station and the mobile transmitter $\phi_{\text{bs}}$. The angle $\phi_{\text{bs}}$ can be calculated using the GPS coordinates of the base station and the mobile transmitter with respect to the view direction of the base station. The angular difference

$$\Delta \phi = |\phi_{\text{bs}} - \hat{\phi}_{\text{max}}|$$

equals zero for scenarios with a dominant LOS path but can have an arbitrary value for NLOS scenarios. This means that the angular difference $\Delta \phi$ can give information about whether the scenario is LOS dominated. In principle, multiple AoAs can be extracted from the estimated and calibrated channel matrix, by analyzing the radiation characteristic including all beamforming vectors given by $\hat{U}^H$.

### D. Signal Quality and Performance Metrics

As a measure of the signal quality, the MER representing a quasi SNR is calculated. Before estimating the MER the received symbols are equalized assuming a frame based data transmission with frame length $L_f$ with periodic appearing training symbols as it is common practice in wireless communications [73]. A one tap equalization is applied using as an equalization matrix

$$\Lambda = \frac{1}{T_f} \sum_{k=0}^{L_f-1} \hat{H}_t(\cdot, \cdot, k)$$

where $\hat{H}_t \in \mathbb{C}^{N_{\text{ant}} \times N_{\text{ant}} \times L_f}$ is the result of (14) extended in time domain with sampling times $t = k \cdot T_0$ for $k \in \{0, 1, \ldots, L_f - 1\}$. On the basis of the equalized receive symbols $R_{\text{eq}} \in \mathbb{C}^{N_{\text{ant}} \times N_{\text{ant}} \times L_f}$ the MER averaged over all receivers and all OFDM carriers is defined by

$$\text{MER} = 10 \cdot \log_{10} \left\{ \frac{\sum_{p=0}^{N_{\text{tot}}-1} P_{\text{ref}}(p)}{\sum_{n=1}^{N_{\text{tot}}} \sum_{p=0}^{N_{\text{tot}}-1} \sum_{k=0}^{L_f-1} E(n, p, k)} \right\}$$

with the error matrix

$$E(n, p, k) = |\text{Re}\{T(p)\} - \text{Re}\{R_{\text{eq}}(n, p, k)\}|^2$$

and the normalization matrix

$$P_{\text{ref}}(p) = \text{Re}\{T(p)\}^2 + \text{Im}\{T(p)\}^2$$

following the descriptions in [74]. Furthermore, the MER can be averaged over $L_s = \lfloor L_{\text{tot}}/L_f \rfloor$ subsequent OFDM frames, where $L_{\text{tot}}$ represents the total number of recorded OFDM symbols.

As a performance metric serves the spectral efficiency or maximum achievable sum rate given in bps/Hz and calculated by [75]

$$R = \log_2 \left\{ \left| I_{\text{ant}} + \frac{\gamma}{M_{\text{ant}}} \hat{H} \hat{H}^H \right| \right\}$$

with the normalized channel matrix $||\hat{H}||^2 = N_{\text{ant}} M_{\text{ant}}$. For the SNR at the receiver $\gamma$ we use the calculated MER in the following analysis.

III. OUTDOOR MEASUREMENT SCENARIOS

For the channel measurements we selected three different cell site scenarios to obtain a realistic picture of the wireless propagation channel. The scenarios were chosen due to their variability in foliage coverage, reflective surfaces, denseness of buildings, availability of LOS and NLOS measurement points...
and their angular spread. Within each scenario we positioned the base station at an elevated position with a fixed view direction and elevation angle. The position of the mobile transmitter is varied within a pre-designated measurement area seen from the base station view direction, making an analysis of the different propagation scenarios and view angles to the base station possible. The determination of the exact spatial position of the transmitter and receiver is based on the recorded and over the measurement period averaged GPS data which are manually verified using a map of the scenario. The position deviation is therefore estimated to be less than 2 m. For each measurement position of the mobile transmitter an around 20 s long recording is made. This allows us to analyze the time dependent behavior of the channel, as for example the influence of foliage movement within the propagation paths. In total 159 measurements are performed and evaluated.

The measurements are performed on several days from May to July causing a high amount of foliage within the surrounding area. During the measurements the weather was partly cloudy and dry. Three different small cell site scenarios were picked for comparison at Campus South of the Karlsruhe Institute of Technology (KIT). For each cell site scenario the elevation and azimuth view direction of the base station is adjusted upfront to cover the desired area best possible. The scenarios are marked in the satellite image in Fig. 3. The image shows the respective position of the base station (B1, B2, and B3), their view directions and the angular ranges of ±60° around the view directions. The different cell sites can be described as follows:

1) Scenario I: In the first scenario the base station is adjusted to cover an open courtyard, which is characterized by a small lake surrounded by buildings on its three sides serving as possible reflective surfaces. Furthermore, a fair amount of foliage belonging to tall trees in the center of the courtyard was present. These blocked a direct LOS propagation between base station and the mobile transmitter at some of the measurement locations, which shows a significant impact on the signal-to-noise ratio (SNR). At the furthermost end of the courtyard, two small building-canyons run on either side of a building, possibly creating highly reflective environments. Additionally, some parked cars prevented the direct LOS path. The base station is positioned on the balcony of an adjacent building in 13 m height and the antenna array is tilted downwards in elevation by 12° from the horizontal view direction.

2) Scenario II: The second scenario covers an intersection and is dominated by heavy foliage spread over a wide angular range, as shown on the right side of the satellite image in Fig. 3. The base station is thereby placed on the roof top of a building in 17 m height and tilted in elevation by 15° downwards from the horizontal view direction. The heavy foliage coverage, is blocking the LOS path at multiple measurement locations, giving possibility to further investigate the influences of foliage onto the propagation channel. Compared to the first cell site scenario, a less reflective environment is present, with a wide street running through the scenario lined by trees and parked cars. Furthermore, occasional wind

3) Scenario III: In the third scenario the base station is placed on a balcony in 35 m height and the antenna array is tilted downwards in elevation by 28° from the horizontal view direction. This scenario comprises few trees, which in combination with the base station height is leading to measurement distances up to 162 m. Here, urban NLOS propagation scenarios are present at several measurement locations.

The key figures of the different cell site scenarios are summarized in Tab. I. To enable a realistic mobile communication scenario, the antennas of the mobile transmitter are placed at a height of 115 cm in all scenarios to emulate the typical height of a cell phone carried by a user. Moreover, the height of the base stations are chosen following the urban micro and macro cell scenarios with high user density identified by 3GPP in [76]. Due to a maximum distance of 162 m within the measurements, the atmospheric gap around 28 GHz and the absence of rain during our measurements, the additional atmospheric path losses can be neglected [77].

IV. CHANNEL MEASUREMENT RESULTS

In the following section the results of the channel measurements are presented. The system parameters used for our measurements are given in Tab. II. The considerably narrow bandwidth is selected to ensure a frequency-nonselective channel behavior. It should be noted, that the presented measurements focus on estimating snapshots of the complex MIMO channel matrix. For more information about the broadband channel behavior or other characteristics as for example power delay profiles we refer to the measurement results presented in [16], [18], [50], [52], [78]. Nevertheless, it is generally possible to use the demonstrator for broadband channel measurements as the designed RF frontends cover the full n257-band. For this purpose, the IF frequency can be varied in time by controlling the utilized SDRs and thus a wide frequency range can be investigated. However, this presupposes a stationary channel over the entire measurement. The modular design also allows the replacement of the bandwidth limiting antennas and SDRs by analog-to-digital converter (ADC) and digital-to-analog converter (DAC) boards with higher sampling rates and processing speeds.

At first, the average MER over the full recording is calculated for each transmitter position and color-coded displayed
paths, which lead to large path losses at 28 GHz. For good propagation scenarios MER values of up to 26 dB could be reached. These values are achieved without using any antenna array gain, i.e. an EIRP of 11.5 dBm, due to the employed channel estimation technique. The MER values therefore look quite promising for future 28 GHz MIMO mobile communication systems. As expected, the highest values could be reached in short distance LOS scenarios at or close to the view direction of the base station. The group of measurement locations marked as \( g_1 \) in Fig. 3 shows multiple LOS measurements with different distances between the base station and the mobile transmitter ranging from 64 m to 150 m. The elevation angle decreases thereby from 33° to 13° the further the transmitter moves away from the base station. The measurements show that the MER only slightly decreases with distance, as a lower elevation angle between the base station and the mobile transmitter leads to a higher antenna element gain at the transmitter and receiver side. Moreover, foliage losses can be estimated using the furthermost point of \( g_1 \) and comparing it with the measurement position of \( g_2 \).

Note that a slight difference in distance for both locations has only a minor impact on the path loss and thereby MER. The measurements show a difference in MER of 9.5 dB due to foliage in the LOS path. Measurement group \( g_3 \) indicates that the MIMO system can successfully operate within a high angular range in azimuth of above 60° achieving MER values of up to 17 dB. The measurement positions summarized in \( g_4 \) have no direct LOS connection to the base station, as the
mobile transmitter was shadowed by the adjacent building. Interesting is the comparison with the measurement positions in $g_5$ made on the other side of the street enabling a LOS connection. The difference in MER between both groups is roughly $8.5 \text{dB}$, showing the stronger path loss of NLOS propagation scenarios. Nevertheless, the difference in MER in the NLOS connection of measurement position $g_6$ and the LOS connection of measurement position $g_7$ is only $0.2 \text{dB}$. This low loss in the NLOS case results from high building fronts surrounding the mobile transmitter like a canyon, which enables the propagation towards the base station. The high influence of the vegetation like trees and bushes onto the path loss can be shown in group $g_8$, where a high number of spatially close measurements have been made showing a high range of MER values varying between $16 \text{dB}$ and $22 \text{dB}$.

To analyze if the wireless propagation channel is LOS or NLOS dominant the histogram of the angular difference $\Delta \phi$ calculated by (21) is depicted in Fig. 4 including all mobile transmitter positions. The result shows a LOS dominance within the measurements made. The reasons for this are not only the selection of the mobile transmitter locations, but also the fact that the likelihood for multipath propagation decreases compared to frequencies below $6 \text{GHz}$. This is caused by the higher path losses and absorption by possible reflectors. Besides the peak around $\Delta \phi = 0^\circ$ the angular difference is spread over the whole range. Note that due to the limited number of measurements not every angular difference is present in Fig. 4.

To analyze the multipath nature of the wireless propagation channel in detail Fig. 5 provides the cumulative distribution function (CDF) of the four eigenvalues of the channel including all mobile transmitter locations. The graph reveals the multipath nature of the wireless propagation channel. It can be seen, that even in this LOS dominated cell site scenarios in $50\%$ of the cases the second eigenvalue is not more than $10 \text{dB}$ lower than the strongest one. Moreover, in $10\%$ of the cases the difference between the strongest and weakest eigenvalue is less than $14 \text{dB}$.

For a deeper understanding of the multipath behavior of the $28 \text{GHz}$ propagation channel, taking a closer look at the difference between the first and second eigenvalue $\Delta \sigma_{1,2}$ is of interest. In Fig. 6 the eigenvalue difference is plotted over the MER for all locations of the mobile transmitter. The eigenvalue difference is averaged in time over the full recording. Furthermore, the distance between the base station and mobile transmitter is color-encoded onto the measurement points. Fig. 6 shows that for low MER values the differences between the first and second eigenvalues of the channel are low. This can be explained by the type of scenario causing the low MER. These scenarios mostly have no LOS connection and the distance between the base station receiver and the mobile transmitter is color-encoded into the graph.

Fig. 4. Statistic of the angular difference $\Delta \phi$ between the physical azimuth angle and the main azimuth beam direction over all mobile transmitter positions in all three cell site scenarios.

Fig. 5. Cumulative distribution function of the normalized eigenvalues of the channel including all mobile transmitter locations of all cell site scenarios.

Fig. 6. Difference between the first and second eigenvalue of the channel $\Delta \sigma_{1,2}$ versus the average MER. The distance between the base station receiver and the mobile transmitter is color-encoded into the graph.
exist, which can be exploited for spatial multiplexing or diversity transmission.

To investigate the achievable spectral efficiency in the presented mobile communication scenarios, the spectral efficiency for all mobile transmitter positions and all scenarios is depicted in Fig. 7. Additionally the course of the spectral efficiency is approximated as a third order polynomial function using the measurement data. While the spectral efficiency increases with an increasing MER, the uncertainty also rises. This behavior is in line with the observations made in Fig. 6. For high MER values the scenario may have only one dominant LOS path leading to a low spectral efficiency, as only the first eigenvalue contributes to the transmission. The spectral efficiency in this case is dominated by the eigenvalue distribution. At low MER values all eigenvalues are highly attenuated, which means that the spectral efficiency is dominated by the MER. As for wider bandwidths additional frequency selective distortions will reduce the signal quality, the presented results of the narrowband achievable spectral efficiency can be used as an indicator for the reachable performance. This helps designers of broadband communication systems to put the achieved spectral efficiency into perspective and indicates the amount of additional interference caused by broadband data transmission.

Next, the time-dependent behavior of the propagation channel is analyzed. For this the beamforming matrices resulting from SVD may be applied to time delayed instances of the channel matrix. Note that in real communication scenarios the channel estimate is used during the transmission of the full frame until the channel estimation is updated, utilizing non-continuous channel estimation approaches. This processing is valid as long as the coherence time is much larger than the frame duration or channel estimation update time. To evaluate the time-dependent behavior, the CDF of the spectral efficiency is calculated for a slow changing and fast changing environment shown in Fig. 8. In each case different frame durations given in multiples of the OFDM symbol duration are used. Note that as the channel is changing, the employed outdated beamforming matrix could also lead to an improvement in spectral efficiency. This is caused by a general improvement of the eigenvalues or MER occurring over time. To illustrate the loss in spectral efficiency by using a time delayed beamforming matrix, the spectral efficiency is calculated for each channel matrix with delayed versions of the beamforming matrices. This indicates the difference between the time-delayed beamforming matrix and the optimum spectral efficiency, which can be reached at this point in time. Note that the minimum delay time is limited by the OFDM symbol duration $T_o = 128 \mu s$. For a scenario with a long coherence time we selected the measurement point marked as $g_9$ within Fig. 3. The communication link is dominated by a LOS connection with an average MER of 16.7 dB and no foliage between the base station and mobile transmitter. The results in Fig. 8(a) show a slow degradation in spectral efficiency with increasing estimation delay. This means the channel is changing slowly over time. Even for a high delay time of $\tau = 16.2 ms$ a drop in spectral efficiency of only 1.2 bps/Hz is reached in 90% of the cases. In contrast, the measurement point marked as $g_{10}$ within Fig. 3 is analyzed, showing an average MER of 9.3 dB. Within this propagation scenario the LOS path is covered by dense foliage, which
rapidly changed the channel over time due to motions of leaves from the wind present that day. The difference is visualized in Fig. 8(b). Already after $\tau = 128 \mu s$ the wireless propagation channel and thereby the ideal beamforming matrix changed drastically leading to a drop of 8 bps/Hz in 90% of the cases. Nevertheless, a saturation effect is visible caused by the static non-variant parts in the propagation environment.

V. CONCLUSION

This work presents a measurement-based analysis of the wireless propagation channel around 28 GHz using a MIMO measurement system. Overall, 159 channel measurements at static mobile transmitter positions have been performed in three realistic small cell site scenarios. The spatial diversity of the channel is analyzed, showing less than 10 dB attenuation of the second path in 50% of the cases, which show the possibility for spatial multiplexing techniques in future mobile communication scenarios at the edge of the mmWave regime. Moreover, the significant influences of moving foliage are investigated and their effects on the achievable spectral efficiency indicate the constraints for data frame durations. The channel sounder enables an estimation of the complex MIMO channel matrix, which can be fed into numerical simulations to investigate MIMO architectures and algorithms.

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REFERENCES


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